# A High Step-Up/Step-Down LVS-Parallel HVS-Series ZVS Bidirectional Converter With Coupled Inductors 

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#### Abstract

This paper introduces a non-isolated bidirectional converter with high-voltage conversion ratio. In the proposed converter, by integrating the two-phase LVS-parallel HVS-series bidirectional converter with the coupled inductors, features such as high voltage-gain, low voltage stresses, current sharing, and current-ripple-cancellation are achieved. Due to the proposed converter's operation in triangular conduction mode, the desirable benefits of zero voltage switching, diode reverse recovery elimination, and reduction of converter filter inductors and, consequently, leakage inductors are obtained. To recycle the leakage inductors' energy and to solve the related difficulties for both operation modes, a simple passive clamp with the minimum number of elements is utilized. Also, to improve the light-loads' efficiency, the variable frequency control is developed. The proposed converter is comprehensively analyzed, and to verify the analysis, the experimental results are provided.


Index Terms-Non-isolated bidirectional converter (BDC), High step-up/step-down converter, LVS-parallel HVS-series converter, Zero voltage switching (ZVS)

## I. Introduction

IN the past decades, the development of renewable energy systems, hybrid/electric vehicles (EVs/HEVs), and uninterruptible power supplies (UPSs) are among the most attractive topics in power electronics. DC-DC bidirectional converters (BDCs) are one of the key components in such applications [1], [2], [3] with the important functions of managing the charge and discharge of batteries and handling the voltage difference between batteries and the DC bus. Applying the battery cells in series connection is usually avoided due to the difficulties such as charge imbalance between the series battery cells and the need for additional battery voltage-balancing circuits [4]. As a solution, the high step-up/step down BDCs are utilized to match the low-voltage battery with the highvoltage DC bus.

Compared with unidirectional high-step-up or high-stepdown converters, the design of high step-up/step-down BDCs faces more challenges, due to two operation modes in opposite directions. Since the low-voltage-side (LVS) source is commonly batteries, providing the continuous-non-pulsating LVS current with a low ripple to maintain the battery life-time is necessary [5]. Furthermore, the current level of LVS is high, and important issues such as conduction losses and thermal management should be taken into consideration.

The LVS-parallel high-voltage-side (HVS)-series structures are among the most favorable circuit structures to address the aforementioned challenges [6]. In these structures, the
converter is normally based on parallel-interleaved converters to obtain excellent features such as current sharing and current-ripple-cancellation. Moreover, each phase's HVS terminals are electrically placed in series to increase the voltage-gain and reduce the components' voltage stress.

In a general classification, the BDCs can be divided into isolated BDCs and non-isolated BDCs. In isolated converters, the converter transformer processes all the output power, which causes increased transformer volume and losses. Moreover, many of the isolated topologies such as dual-active-bridge (DAB) converters, as the most common structure of isolated BDCs, require high number of active switches [7], [8]. Hence, when isolation is not a requirement, non-isolated BDCs are usually preferred.

Utilizing the coupled-inductor with the converter filterinductor (i.e. coupled-filter-inductor) is the most common method to increase the voltage-gain in non-isolated BDCs [9]-[20], and is also common in non-isolated unidirectional structures [21]. This method is also integrated with other switched-capacitor circuits to increase the voltage-gain and recycle the leakage inductor energy [9]-[18]. In these converters, unlike the isolated BDCs, only a portion of output power is processed through the coupled inductors. Besides, as the magnetizing inductor of the coupled inductors plays the filter inductor's role, the core reset is not an issue. In the BDCs with coupled-filter-inductor, by properly controlling the converter, the leakage inductor energy could be utilized to achieve zero-voltage-switching (ZVS) [10]-[18].

The general drawback of BDCs with coupled-filter-inductor is the large current-ripple and/or pulsating state of LVS current due to the coupled inductor on the converter filter inductor [10]-[19]. As a solution, it is necessary to utilize the bulky low-pass filter on the converter's high-current LVS, which increases the converter volume and conduction losses [9]. The reference [20] introduces a two-phase interleaved structure with current-ripple-cancellation featuring the continuous-low-ripple current on LVS. However, recycling the leakage inductors' energy is the main issue in this converter, which is solved with many auxiliary components, including four separate clamp circuit without achieving ZVS condition. In [22], [23], the single-phase BDCs with coupled-filter-inductor are introduced, featuring low LVS-current-ripple. However, these converters suffer from limited voltage-gain since the coupled inductors are merely utilized to obtain current-ripplecancellation, and the voltage-gain is independent of the cou-
pled inductors' wingdings turn ratio.
In high step-up/step down BDCs with coupled inductors proposed in [24]-[29], the coupled inductors are implemented separately from the converter filter inductor (i.e., built-in transformer). Therefore, the LVS current benefits from continuous state and low-ripple. Besides, in [24]-[26], this method is utilized with the parallel-interleaved structure. However, in [29], the voltage-stress of all switches are more than the voltage level of HVS, and BDCs in [27], [28] suffer from limited voltage-gain. Moreover, despite the benefits of proposed converters in [24]-[26], they utilize high number of components including eight [24], [25] and six [26] active switches.

In BDCs [30]-[42], the high voltage-gain is obtained without using the coupled inductors, and thus, the related mentioned issues with the coupled inductors do not exist in these converters. These converters are based on integrating the basic BDCs with the switched-capacitor or quasi-Z-source circuits [31]-[42]. Generally, the voltage-gains of these converters are limited, and to increase the voltage-gain, additional circuit cells are required [32], [33], which increases the converter's volume. This is in contrast with the coupled inductors BDCs, where the voltage-gain could be increased by increasing the windings turns ratio, considering the value of the leakage inductor and the associated issues. Besides, the pulsed-current related to parallel unbalanced-voltage capacitors in switchedcapacitor circuits should be addressed as it requires the large value capacitors to alleviate this issue [33]-[42]. The other drawback of these converters is that most of them are hard-switched [31]-[42]. This issue limits the converter switching frequency, especially when the conventional Silicon MOSFETs are utilized as their body diodes commonly suffer from the large reverse-recovery-time [43], [44]. It worths mentioning that in BDCs, the antiparallel diodes of switches mostly operate as the converter main diodes.

The triangular conduction mode (TCM) operation is among the simplest methods to obtain soft switching in BDCs [22], [45], [46]. In this method, the main inductor of the converter is designed small enough such that its current flows in both directions. This way, ZVS condition, elimination of diodes-reverse-recovery losses, and reduction of main inductances can be obtained [22]. However, due to the large current ripple of main inductors, both the converter's conduction losses and core losses are increased. These losses are almost constant regardless of the output power in fixed-frequency operation; hence, the value of these losses would be dominant in light loads, results in dropped efficiency in this region [22]. Moreover, the regular BDCs with single-phase structure in TCM suffer from a large current ripple on the LVS source [45].

This paper introduces a two-phase LVS-parallel HVS-series TCM bidirectional converter with coupled inductors to address the existing solutions' issues. Thanks to the LVS-parallel HVSseries structure, the current sharing is achieved, voltage-gain is increased, and the voltage stresses are reduced. Furthermore, the coupled inductors' secondary windings are jointly implemented on the common path of two phases in the form of winding-cross-coupled-inductors (WCCIs) [47]. As a result, excellent voltage-gain and current-ripple-cancellation


Fig. 1. (a) Circuit structure of the proposed converter. (b) Equivalent circuit of the proposed converter.
are achieved utilizing a minimum number of windings. Due to TCM operation and current ripple cancellation, ZVS and elimination of the diodes-reverse-recovery losses are obtained without a large current ripple on the LVS side. Moreover, the converter inductors values, including the leakage inductors' values and the associated issues, are reduced. To completely solve the leakage inductors' difficulties in two phases and both boost and buck operation modes, a simple passive clamp circuit with the minimum number of elements is applied. Furthermore, to reduce losses related to TCM operation in light loads, variable frequency control is adopted in the proposed converter.

The paper is organized as follows. Section II describes the circuit configuration and operation principles of the proposed converter. The proposed converter specifications are discussed in Section III. Section IV provides the design considerations. In Section V, the experimental results, loss analysis, and comparison are presented. Finally, conclusions are mentioned in Section VI.

## II. Circuit Configuration and Operation

Fig. 1(a) shows the circuit configuration of the proposed converter. The converter circuit comprises two phases in which the LVSs of phases are parallel, and the HVSs ( $V_{H 1}$ and $V_{H 2}$ ) are series. The upper phase comprises of the inductor $L_{1}$, the LVS switch $S_{1}$, HVS switch $S_{3}$, and the HVS capacitor $C_{H 1}$. The lower phase includes the inductor $L_{2}$, the LVS switch $S_{2}$, HVS switch $S_{4}$, and the HVS capacitor $C_{H 2}$. Besides, the capacitors $C_{S 1}-C_{S 4}$ are the snubber capacitors of switches.

To increase the voltage-gain and obtain the current-ripplecancellation, the secondary windings of coupled inductors ( $L_{3}$ and $L_{4}$ ) are inserted in the common path of two phases, in the crossed form. The secondary windings of coupled inductors $L_{3}$ and $L_{4}$ contribute to increasing the voltage-gain of both phases. This leads to a reduced number of coupled inductor windings compared to other existing converters with WCCIs [47].

The proposed converter also includes a simple passive clamp circuit, which composes of a single clamp capacitor $C_{C}$ and three diodes, $D_{C 1}, D_{C 2}, D_{C 3}$. The passive clamp has the role of limiting the voltage of the switches $S_{1}$ and $S_{2}$ at both the boost and buck operation modes. Otherwise, during the turnoff instants of $S_{1}$ and $S_{2}$, the stored energy in the leakage inductors is depleted through a resonance with switches output capacitors, causing an undesirable voltage spike on $S_{1}$ and $S_{2}$.

A pair of coupled inductors $L_{1}$ and $L_{2}$ with coupling coefficient $k$, as shown in Appendix A, can be modeled with an ideal transformer with turn ratio $N\left(N=k \sqrt{L_{2} / L_{1}}\right)$, a magnetizing inductor $\left(L_{M}\right)$ on the primary side $\left(L_{M}=L_{1}\right)$, and a leakage inductor $\left(L_{l k}\right)$ on the secondary side ( $L_{l k}=$ $\left(1-k^{2}\right) L_{2}$ ). Fig. 1(b) illustrates the equivalent circuit of the proposed converter using the model. It is worth mentioning that, in the equivalent circuit of the proposed converter, the magnetizing inductors $L_{M 1}$ and $L_{M 2}$ act as the converter filter inductor. Also, the series leakage inductors ( $L_{l k 1}$ and $L_{l k 2}$ ) can be replaced with an equivalent leakage inductor $L_{l k}$ $\left(L_{l k}=L_{l k 1}+L_{l k 2}\right)$.

The proposed converter has two overall operation modes of boost and buck modes, based on whether the power flow direction is from $V_{L}$ to $V_{H}$ or vice versa. Also, each operation mode includes twelve operating intervals, which are discussed below comprehensively. In the analysis, the following assumptions are considered:

- The converter is in the steady-state condition.
- The values of the windings turn ratios are equal $\left(N_{1}=\right.$ $N_{2}=N$ ).
- The converter operates in TCM (the values of magnetizing inductors $L_{M 1}$ and $L_{M 2}$ are small enough such that their currents flow in both directions).
- The values of the HVS capacitors $C_{H 1}$ and $C_{H 2}$, and also the clamp capacitor $C_{C}$ are large enough that their voltages are constant in a switching cycle.
- The voltage drop of the diodes $D_{C 1}, D_{C 2}$ and $D_{C 3}$ during the forward biased condition are equal and defined as $V_{D, \mathrm{ON}}$.


## A. Boost Mode

In the boost mode, $S_{1}$ and $S_{2}$ are the main switches, and $S_{3}$ and $S_{4}$ act as the synchronous switches complementary to $S_{1}$ and $S_{2}$ with a proper dead-time. Also, two phases operate with interleaved pattern and there is a phase-shift of $180^{\circ}$ between them. The equivalent circuits of twelve operating intervals in boost mode, and the theoretical key waveforms are illustrated in Figs. 2 and 3, respectively.

At the beginning of interval 1 , it is assumed that the value of $i_{L M 1}$ is $I_{0}$, and $i_{L M 2}$ has a negative value of $-I_{0}^{\prime}$. Also,
it is assumed that $S_{1}$ is ON , and the body diode of $S_{2}$ is conducting.

Interval $1\left[t_{0}-t_{1}\right]$ : In this interval and by conducting the $S_{2}$ body diode, $S_{2}$ turns ON under ZVS. During this interval, the voltage of $V_{L}$ is placed across $L_{M 1}$ and $L_{M 2}$. Hence, $i_{L M 1}$ increases linearly, and $i_{L M 2}$ reduces linearly in the negative direction, as follows:

$$
\begin{align*}
i_{L M 1}(t) & =I_{0}+\frac{V_{L}}{L_{M 1}}\left(t-t_{0}\right)  \tag{1}\\
i_{L M 2}(t) & =-I_{0}^{\prime}+\frac{V_{L}}{L_{M 2}}\left(t-t_{0}\right) \tag{2}
\end{align*}
$$

In this interval, the currents of $i_{L M 1}$ and $i_{L M 2}$ conducts through the $S_{1}$ and $S_{2}$, respectively, and there are no currents in the windings of the ideal transformers.

Interval $2\left[t_{1}-t_{2}\right]$ : At $t_{1}, S_{1}$ turns OFF, and the snubber capacitors $C_{S 1}$ and $C_{S 3}$ start to charge and discharge, respectively, by means of $i_{L M 1}$. Meanwhile, a resonance starts between $L_{l k}$ and $C_{S 4}$ causes $C_{S 4}$ charging.

Interval $3\left[t_{2}-t_{3}\right]$ : At $t_{2}, C_{S 1}$ is charged to $V_{C}, D_{C 1}$ is forward biased, and the voltage of $C_{S 1}$ is clamped on $V_{C}$. Hence, the resonance between $L_{l k}$ and $C_{S 4}$ in interval 2 continues in this interval between $L_{l k}, C_{S 4}$, and $C_{S 3}$. During this resonance, $C_{S 3}$ is discharged from $V_{H 1}$ to zero, and $C_{S 4}$ is charged from $V_{H 2}$ to $V_{H}-V_{C}$. At the end of this interval, the values of $i_{L M 1}, i_{L M 2}$ and $i_{L l k}$ are defined $I_{1},-I_{1}^{\prime}$, and $I_{K 0}$, respectively.

Interval $4\left[t_{3}-t_{4}\right]$ : At $t_{3}, S_{3}$ body diode is forward biased. By conducting $S_{3}$ body diode, the synchronous switch $S_{3}$ turns ON under ZVS, and thus, the current of $S_{3}$ body diode conducts through $S_{3}$. In this interval, the voltage of $-\left(V_{C}+V_{D, \text { ON }}-V_{L}\right)$ is placed across $L_{M 1}$, and the voltage of $L_{M 2}$ is $V_{L}$ as yet. Hence, the equations of $i_{L M 1}$ and $i_{L M 2}$ would be:

$$
\begin{gather*}
i_{L M 1}(t)=I_{1}-\frac{V_{C}+V_{D, \mathrm{ON}}-V_{L}}{L_{M 1}}\left(t-t_{3}\right)  \tag{3}\\
i_{L M 2}(t)=-I_{1}^{\prime}+\frac{V_{L}}{L_{M 2}}\left(t-t_{3}\right) \tag{4}
\end{gather*}
$$

Also, the voltage of $(N+1)\left(V_{C}+V_{D, \mathrm{ON}}\right)-V_{H 1}$ is placed across $L_{l k}$, hence, the equation of $i_{L l k}$ is given by:

$$
\begin{equation*}
i_{L l k}(t)=I_{K 0}+\frac{(N+1)\left(V_{C}+V_{D, \mathrm{ON}}\right)-V_{H 1}}{L_{l k}}\left(t-t_{3}\right) \tag{5}
\end{equation*}
$$

At the end of this interval, the value of $i_{L l k}$ is defined $I_{K 1}$. Interval $5\left[t_{4}-t_{5}\right]$ : At $t_{4}$, the current of $C_{C}$ reaches zero, and so, $D_{C 1}$ turns OFF. Then, the current of $C_{C}$ increases in the negative direction through $D_{C 3}$. In this interval, the voltages of $L_{M 1}$ and $L_{M 2}$ are $-\left(V_{C}-V_{D, \mathrm{ON}}-V_{L}\right)$ and $V_{L}$, respectively. Hence, $i_{L M 1}$ and $i_{L M 2}$ continues to reduce and increase, respectively, at almost the same current rates in interval 4. Besides, the voltage of $-\left(V_{H 1}-(N+1)\left(V_{C}-V_{D, \mathrm{ON}}\right)\right)$ is placed across $L_{l k}$. Hence, the equation of $i_{L l k}$ is given by:

$$
\begin{equation*}
i_{L l k}(t)=I_{K 1}-\frac{V_{H 1}-(N+1)\left(V_{C}-V_{D, \mathrm{ON}}\right)}{L_{l k}}\left(t-t_{4}\right) \tag{6}
\end{equation*}
$$



Note: The unlabeled current arrows (red arrows) refer to the actual direction of current.

Fig. 2. Equivalent circuits of twelve operating intervals in boost mode.


Fig. 3. Theoretical key waveforms in boost mode.

At the end of this interval, the value of $i_{L l k}$ is defined $-I_{K 2}$. Interval $6\left[t_{5}-t_{6}\right]$ : At $t_{5}$, the synchronous switch $S_{3}$ turns OFF, and the snubber capacitors $C_{S 1}$ and $C_{S 3}$ start to discharge and charge, respectively, by means of $i_{L M 1}$. Meanwhile, a resonance starts between $L_{l k}$ and $C_{S 4}$ causes $C_{S 4}$ discharging. During this interval, $C_{S 1}$ discharges completely, $C_{S 3}$ charges until $V_{H 1}$, and $C_{S 4}$ discharges from $V_{H}-V_{C}$ to $V_{H 2}$. At the end of this interval, the values of $i_{L M 1}$ and $i_{L M 2}$ are defined $-I_{2}$ and $I_{2}^{\prime}$, respectively.

Interval $7\left[t_{6}-t_{7}\right]$ : At $t_{6}, C_{S 1}$ is discharges, and its body diode turns ON. By conducting the $S_{1}$ body diode, $S_{1}$ turns ON under ZVS. During this interval, the voltage of $V_{L}$ is placed across $L_{M 1}$ and $L_{M 2}$. Hence, $i_{L M 1}$ reduces linearly in the negative direction, and $i_{L M 2}$ increases linearly. In this interval, the currents of $i_{L M 1}$ and $i_{L M 2}$ conducts through the $S_{1}$ and $S_{2}$, respectively, and there are no currents in the windings of the ideal transformers.
Interval $8\left[t_{7}-t_{8}\right]$ : At $t_{7}, S_{2}$ turns OFF, and the snubber capacitors $C_{S 2}$ and $C_{S 4}$ start to charge and discharge, respectively, by means of $i_{L M 2}$. Meanwhile, a resonance starts between $L_{l k}$ and $C_{S 3}$ causes $C_{S 3}$ charging.

Interval $9\left[t_{8}-t_{9}\right]$ : At $t_{8}, C_{S 2}$ is charged to $V_{C}$, and thus,
$D_{C 2}$ is forward biased. In this interval, resonance continues between $L_{l k}, C_{S 3}$, and $C_{S 4}$. During this resonance, $C_{S 4}$ discharges completely, and $C_{S 3}$ charges from $V_{H 1}$ to $V_{H}$. At the end of this interval, the values of $i_{L M 1}, i_{L M 2}$ and $i_{L l k}$ are defined $-I_{3}, I_{3}^{\prime}$, and $-I_{K 3}$, respectively.

Interval 10 [ $\left.t_{9}-t_{10}\right]$ : At $t_{9}, S_{4}$ body diode is forward biased and starts to conduct. By conducting $S_{4}$ body diode, the synchronous switch $S_{4}$ turns ON under ZVS, and so, $S_{4}$ body diode current conducts through $S_{4}$. In this interval, the voltage of $-\left(V_{C}+V_{D, \mathrm{ON}}-V_{L}\right)$ is placed across $L_{M 2}$, and the voltage of $L_{M 1}$ is $V_{L}$ as yet. Hence, the equations of $i_{L M 1}$ and $i_{L M 2}$ would be:

$$
\begin{gather*}
i_{L M 1}(t)=-I_{3}-\frac{V_{L}}{L_{M 1}}\left(t-t_{9}\right)  \tag{7}\\
i_{L M 2}(t)=I_{3}^{\prime}+\frac{V_{C}+V_{D, \mathrm{ON}}-V_{L}}{L_{M 2}}\left(t-t_{9}\right) . \tag{8}
\end{gather*}
$$

Also, the voltage of $V_{H 2}-(N+1)\left(V_{C}+V_{D, \mathrm{ON}}\right)$ is placed across $L_{l k}$, hence, the equation of $i_{L l k}$ is obtained as follows:

$$
\begin{equation*}
i_{L l k}(t)=-I_{K 3}+\frac{V_{H 2}-(N+1)\left(V_{C}+V_{D, \mathrm{ON}}\right)}{L_{l k}}\left(t-t_{9}\right) \tag{9}
\end{equation*}
$$

At the end of this interval, the value of $i_{L l k}$ is defined $-I_{K 4}$.
Interval $11\left[t_{10}-t_{11}\right]$ : At $t_{10}$, the current of $C_{C}$ reaches zero, and so, $D_{C 2}$ turns OFF. In this interval, the voltage of $L_{M 1}, L_{M 2}$ and $L_{l k}$ are $V_{L},-\left(V_{C}+V_{D, \mathrm{ON}}-V_{L}\right)$, and $V_{H 2}-$ $(N+1)\left(V_{C}+V_{D, \mathrm{ON}}\right)$, respectively. Hence, $i_{L M 1}$ increases linearly, $i_{L M 2}$ reduces linearly, and $i_{L l k}$ reduces linearly in the negative direction, at the same current rates in interval 10. At the end of this interval, the value of $i_{L l k}$ is defined $I_{K 5}$.

Interval $12\left[t_{11}-\left(t_{0}+T\right)\right]$ : At $t_{11}$, the synchronous switch $S_{4}$ turns OFF, and the snubber capacitors $C_{S 2}$ and $C_{S 4}$ start to discharge and charge, respectively, by means of $i_{L M 2}$. Meanwhile, a resonance starts between $L_{l k}$ and $C_{S 3}$ causes $C_{S 3}$ discharging. During this interval, $C_{S 2}$ discharges completely, $C_{S 4}$ charges until $V_{H 2}$, and $C_{S 3}$ discharges from $V_{H}$ to $V_{H 1}$. At the end of this interval, the values of $i_{L M 1}$ and $i_{L M 2}$ are defined $I_{0}$ and $-I_{0}^{\prime}$, respectively, and the next switching cycle begins.

## B. Buck Mode

In the Buck mode, $S_{3}$ and $S_{4}$ are the main switches, and the switches $S_{1}$ and $S_{2}$ act as the synchronous switches in the complementary with $S_{3}$ and $S_{4}$, considering a sufficient deadtime. Also, two phases operate with interleaved pattern and there is a phase-shift of $180^{\circ}$ between them. The equivalent circuits of twelve operating intervals in buck mode, and the theoretical key waveforms are illustrated in Figs. 4 and 5, respectively.

At the beginning of interval 1 , it is assumed that $i_{L M 1}$ has a negative value of $-I_{0}$, and the value of $i_{L M 2}$ is $I_{0}^{\prime}$. Also, it is assumed that $S_{1}$ is ON , and the body diode of $S_{2}$ is conducting.

Interval $1\left[t_{0}-t_{1}\right]$ : In this interval and by conducting the $S_{2}$ body diode, the synchronous switch $S_{2}$ turns ON under ZVS, and so, $S_{2}$ body diode current conducts through $S_{2}$. During
this interval, the voltage of $-V_{L}$ is placed across $L_{M 1}$ and $L_{M 2}$. Hence, $i_{L M 1}$ increases linearly in the negative direction, and $i_{L M 2}$ reduces linearly, as follows:

$$
\begin{align*}
& -i_{L M 1}(t)=-I_{0}-\frac{V_{L}}{L_{M 1}}\left(t-t_{0}\right)  \tag{10}\\
& -i_{L M 2}(t)=I_{0}^{\prime}-\frac{V_{L}}{L_{M 2}}\left(t-t_{0}\right) \tag{11}
\end{align*}
$$

In this interval, the currents of $-i_{L M 1}$ and $-i_{L M 2}$ conducts through the $S_{1}$ and $S_{2}$, respectively, and there are no currents in the windings of the ideal transformers.

Interval $2\left[t_{1}-t_{2}\right]$ : At $t_{1}$, the synchronous switch $S_{1}$ turns OFF, and the snubber capacitors $C_{S 1}$ and $C_{S 3}$ start to charge and discharge, respectively, by means of $i_{L M 1}$. Meanwhile, a resonance starts between $L_{l k}$ and $C_{S 4}$ causes $C_{S 4}$ charging.

Interval $3\left[t_{2}-t_{3}\right]$ : At $t_{2}, C_{S 4}$ is charged to $V_{H}-V_{C}$, and thus, $D_{C 3}$ is forward biased. In this interval, resonance continues between $L_{l k}, C_{S 1}$, and $C_{S 3}$. During this resonance, $C_{S 3}$ discharges completely, and $C_{S 1}$ charges to $V_{C}$. At the end of this interval, the values of $-i_{L M 1},-i_{L M 2}$ and $i_{L l k}$ are defined $-I_{1}, I_{1}^{\prime}$, and $I_{K 0}$, respectively.

Interval $4\left[t_{3}-t_{4}\right]$ : At $t_{3}, S_{3}$ body diode is forward biased. By conducting $S_{3}$ body diode, $S_{3}$ turns ON under ZVS. In this interval, the voltage of $V_{C}-V_{D, \mathrm{ON}}-V_{L}$ is placed across $L_{M 1}$, and the voltage of $L_{M 2}$ is $-V_{L}$ as yet. Hence, the equations of $-i_{L M 1}$ and $-i_{L M 2}$ would be:

$$
\begin{gather*}
-i_{L M 1}(t)=-I_{1}+\frac{V_{C}-V_{D, \mathrm{ON}}-V_{L}}{L_{M 1}}\left(t-t_{3}\right)  \tag{12}\\
-i_{L M 2}(t)=I_{1}^{\prime}-\frac{V_{L}}{L_{M 2}}\left(t-t_{3}\right) \tag{13}
\end{gather*}
$$

Also, the voltage of $-\left(V_{H 1}-(N+1)\left(V_{C}-V_{D, \mathrm{ON}}\right)\right)$ is placed across $L_{l k}$, and $i_{L l k}$ reduces linearly from $I_{K 0}$. Hence, the equation of $i_{L l k}$ is given by:

$$
\begin{equation*}
i_{L l k}(t)=I_{K 0}-\frac{V_{H 1}-(N+1)\left(V_{C}-V_{D, \mathrm{ON}}\right)}{L_{l k}}\left(t-t_{3}\right) \tag{14}
\end{equation*}
$$

At the end of this interval, the value of $i_{L l k}$ is defined $I_{K 1}$. Interval $5\left[t_{4}-t_{5}\right]$ : At $t_{4}$, the current of $C_{C}$ reaches zero, and so, $D_{C 3}$ turns OFF. In this interval, similar to interval 4, the voltage of $L_{M 1}, L_{M 2}$ and $L_{l k}$ are $V_{C}-V_{D, \mathrm{ON}}-V_{L},-V_{L}$, and $-\left(V_{H 1}-(N+1)\left(V_{C}-V_{D, \mathrm{ON}}\right)\right)$, respectively. Hence, $-i_{L M 1}$ increases linearly, $-i_{L M 2}$ reduces linearly, and $i_{L l k}$ reduces linearly, at the same current rates in interval 4. At the end of this interval, the values of $i_{L l k}$ is defined $-I_{K 2}$.

Interval $6\left[t_{5}-t_{6}\right]$ : At $t_{5}, S_{3}$ turns OFF, and the snubber capacitors $C_{S 1}$ and $C_{S 3}$ start to discharge and charge, respectively, by means of $-i_{L M 1}$. Meanwhile, a resonance starts between $L_{l k}$ and $C_{S 4}$ causes $C_{S 4}$ discharging. During this interval, $C_{S 1}$ discharges completely, $C_{S 3}$ charges until $V_{H 1}$, and $C_{S 4}$ discharges from $V_{H}-V_{C}$ to $V_{H 2}$. At the end of this interval, the values of $-i_{L M 1}$ and $-i_{L M 2}$ are defined $I_{2}$ and $-I_{2}^{\prime}$, respectively.

Interval $7\left[t_{6}-t_{7}\right]$ : At $t_{6}, S_{1}$ body diode is forward biased and starts to conduct. By conducting $S_{1}$ body diode, the


Note: The unlabeled current arrows (red arrows) refer to the actual direction of current.

Fig. 4. Equivalent circuits of twelve operating intervals in buck mode.


Fig. 5. Theoretical key waveforms in buck mode.
synchronous switch $S_{1}$ turns ON under ZVS, and so, $S_{1}$ body diode current conducts through $S_{1}$. During this interval, the voltage of $-V_{L}$ is placed across $L_{M 1}$ and $L_{M 2}$. Hence, $-i_{L M 1}$ reduces linearly, and $-i_{L M 2}$ increases linearly in the negative direction. In this interval, the currents of $-i_{L M 1}$ and $-i_{L M 2}$ conducts through the $S_{1}$ and $S_{2}$, respectively, and there are no currents in the windings of the ideal transformers.
Interval $8\left[t_{7}-t_{8}\right]$ : At $t_{7}, S_{2}$ turns OFF, and the snubber capacitors $C_{S 2}$ and $C_{S 4}$ start to charge and discharge, respectively, by means of $-i_{L M 2}$. Meanwhile, a resonance starts between $L_{l k}$ and $C_{S 3}$ causes $C_{S 3}$ charging.

Interval $9\left[t_{8}-t_{9}\right]$ : At $t_{8}, C_{S 2}$ is charged to $V_{C}$, and thus, $D_{C 2}$ is forward biased. In this interval, resonance continues between $L_{l k}, C_{S 3}$, and $C_{S 4}$. During this resonance, $C_{S 4}$ discharges completely, and $C_{S 3}$ charges to $V_{H}$. At the end of this interval, the values of $-i_{L M 1},-i_{L M 2}$ and $i_{L l k}$ are defined $I_{3},-I_{3}^{\prime}$, and $-I_{K 3}$, respectively.

Interval $10\left[t_{9}-t_{10}\right]$ : At $t_{9}, S_{4}$ body diode and $D_{C 2}$ are forward biased and starts to conduct. By conducting $S_{4}$ body diode, $S_{4}$ turns ON under ZVS. In this interval, the voltage of $V_{C}+V_{D, \mathrm{ON}}-V_{L}$ is placed across $L_{M 2}$, and the voltage of $L_{M 1}$ is $-V_{L}$ as yet. Hence, the equations of $-i_{L M 1}$ and
$-i_{L M 2}$ would be:

$$
\begin{gather*}
-i_{L M 1}(t)=I_{3}-\frac{V_{L}}{L_{M 1}}\left(t-t_{9}\right),  \tag{15}\\
-i_{L M 2}(t)=-I_{3}^{\prime}+\frac{V_{C}+V_{D, \mathrm{ON}}-V_{L}}{L_{M 2}}\left(t-t_{9}\right) . \tag{16}
\end{gather*}
$$

Also, the voltage of $V_{H 2}-(N+1)\left(V_{C}+V_{D, \mathrm{ON}}\right)$ is placed across $L_{l k}$, hence, the equation of $i_{L l k}$ is obtained as follows:

$$
\begin{equation*}
i_{L l k}(t)=-I_{K 3}+\frac{V_{H 2}-(N+1)\left(V_{C}+V_{D, \mathrm{ON}}\right)}{L_{l k}}\left(t-t_{9}\right) \tag{17}
\end{equation*}
$$

At the end of this interval, the value of $i_{L l k}$ is defined $-I_{K 4}$.
Interval $11\left[t_{10}-t_{11}\right]$ : At $t_{10}$, the current of $C_{C}$ reaches zero, and so, $D_{C 2}$ turns OFF. In this interval, similar to interval 10, the voltages of $L_{M 1}, L_{M 2}$ and $L_{l k}$ are $-V_{L}, V_{C}+V_{D, \mathrm{ON}}-$ $V_{L}$, and $V_{H 2}-(N+1)\left(V_{C}+V_{D, \mathrm{ON}}\right)$, respectively. Hence, $-i_{L M 1}$ reduces linearly, $-i_{L M 2}$ increases linearly, and $i_{L l k}$ increases linearly, at the same current rates in interval 10. At the end of this interval, the value of $i_{L l k}$ is defined $I_{K 5}$.

Interval $12\left[t_{11}-\left(t_{0}+T\right)\right]$ : At $t_{11}, S_{4}$ turns OFF, and the snubber capacitors $C_{S 2}$ and $C_{S 4}$ start to discharge and charge, respectively, by means of $-i_{L M 2}$. Meanwhile, a resonance starts between $L_{l k}$ and $C_{S 3}$ causes $C_{S 3}$ discharging. During this interval, $C_{S 2}$ discharges completely, $C_{S 4}$ charges until $V_{H 2}$, and $C_{S 3}$ discharges from $V_{H}$ to $V_{H 1}$. At the end of this interval, the values of $-i_{L M 1}$ and $-i_{L M 2}$ are defined $-I_{0}$ and $I_{0}^{\prime}$, respectively, and the next switching cycle begins.

## III. Converter Specifications

This section describes the key specifications of the proposed converter, including the voltage-gain, stresses of the switches, and the current ripple cancellation. For this purpose, the following assumptions are considered in the analysis:

- The operating duty-cycle in boost mode (duty cycle of $S_{1}$ and $S_{2}$ ) and buck mode (duty cycle of $S_{3}$ and $S_{4}$ ) are $D$ and $D^{\prime}$, respectively.
- The resonance intervals (intervals 2, 3, 6, 8, 9, and 12) are very short, and these intervals are omitted in the analysis. Besides, the voltage drop of the diodes is omitted here $\left(V_{D, \mathrm{ON}}=0\right)$. Based on these simplifications, some of the required simplified waveforms of the proposed converter in boost mode are shown in Fig. 6.


## A. Voltage-Gain and Voltage Stress of Semiconductors

In the steady-state condition, the average voltage across each converter inductor is equal to zero (i.e., volt-second balance). Considering this fact, and from the simplified waveform of $v_{L M 1}$ (or $v_{L M 2}$ ) in Fig. 6, the value of $V_{C}$ is derived as

$$
\begin{equation*}
V_{C}=\frac{V_{L}}{1-D} \tag{18}
\end{equation*}
$$

Also, due to the almost symmetrical operation of the proposed converter, we have $V_{H 1}=V_{H 2}$. Hence, considering that $V_{H 1}+V_{H 2}=V_{H}$, the following equation would be obtained:


Fig. 6. Simplified waveforms of the proposed converter in boost mode.

$$
\begin{equation*}
V_{H 1}=V_{H 2}=\frac{V_{H}}{2} \tag{19}
\end{equation*}
$$

From equivalent circuit of interval 11 in boost mode (See Fig. 2), and using the KVL and KCL laws, we have $-V_{L}+$ $L_{M 2} \frac{d i_{L M 2}}{d t}-N V_{C}-L_{l k} \frac{d i_{L l k}}{d t}+V_{H 2}=0$ and $i_{L M 2}=-(N+$ 1) $i_{L l k}$. Using these equations, and also from (18), (19), (42), (43), and (44), the voltage-gain of the proposed converter in boost mode would be obtained as:

$$
\begin{equation*}
\frac{V_{H}}{V_{L}}=\frac{2(1+N)-D \alpha}{1-D} \tag{20}
\end{equation*}
$$

where, $\alpha$ is given by

$$
\begin{equation*}
\alpha=\frac{2 N^{2}\left(1-k^{2}\right)}{(N+1) k^{2}} \tag{21}
\end{equation*}
$$

Similarly, in the buck mode and considering the value of $\alpha$ given by (21), the voltage-gain is derived as:

$$
\begin{equation*}
\frac{V_{L}}{V_{H}}=\frac{D^{\prime}}{2(N+1)-\left(1-D^{\prime}\right) \alpha} \tag{22}
\end{equation*}
$$

Based on (20), (21), and (22), the voltage-gain of the proposed converter versus duty-cycle for different values of $k$ considering $N=1$ are plotted in Fig. 7(a).

In an ideal case that coupling is complete $(k=1)$, from (21), the value of $\alpha$ would be equal to zero. Hence, from (20) and (22), the voltage-gains in boost and buck modes when $k=1$ are given by (23) and (24), respectively.

$$
\begin{align*}
& \frac{V_{H}}{V_{L}}=\frac{2(1+N)}{1-D}  \tag{23}\\
& \frac{V_{L}}{V_{H}}=\frac{D^{\prime}}{2(N+1)} \tag{24}
\end{align*}
$$

From (23) and (24), the voltage-gain of the proposed converter for different values of $N$ are plotted in Fig. 7(b).

Based on the analysis of the converter operation, the voltage stress of the switches $S_{1}$ and $S_{2}$, and diodes $D_{C 1}$ and $D_{C 2}$ is equal to $V_{C}$. From (18) and (23), the voltage of $V_{C}$, and so, the voltage stress of $S_{1}, S_{2}, D_{C 1}$, and $D_{C 2}$ is derived as:

$$
\begin{equation*}
V_{C}=\frac{V_{H}}{2(N+1)} \tag{25}
\end{equation*}
$$



Fig. 7. (a) Voltage-gain versus duty-cycle for different values of $k(N=1)$. (b) Voltage-gain versus duty-cycle for different values of $N(k=1)$. (c) Voltage stress of switches versus $N(k=1)$.

Moreover, the voltage stress of switch $S_{4}$ and diode $D_{C 3}$ is $V_{H}-V_{C}$. By using the equation (25), the voltage of $V_{H}-V_{C}$, and so, the voltage stress of $S_{4}$ and $D_{C 3}$ is obtained as:

$$
\begin{equation*}
V_{H}-V_{C}=\frac{(2 N+1) V_{H}}{2(N+1)} \tag{26}
\end{equation*}
$$

Finally, the voltage stress of $S_{3}$ is $V_{H}$. Based on the derived equations, the voltage stress of the converter switches versus $N$, considering $k=1$, are plotted in Fig. 7(c).

## B. Current Ripple Cancellation

In the proposed converter, similar to the converters with WCCIs [47], the current-ripple-cancellation is feasible. To illustrate this point, based on the defined currents in Fig. 1(b), the LVS currents of upper phase $\left(i_{L 1}\right)$ and lower phase $\left(i_{L 2}\right)$ are equal to $i_{L M 1}-N_{1} i_{L l k}$ and $i_{L M 2}+N_{2} i_{L l k}$, respectively.

Since the current of LVS $\left(i_{V L}\right)$ is equal to $i_{L 1}+i_{L 2}$, the value of $i_{V L}$ would be obtained as:

$$
\begin{equation*}
i_{V L}=i_{L M 1}+i_{L M 2}-N_{1} i_{L l k}+N_{2} i_{L l k} \tag{27}
\end{equation*}
$$

From (27), if the turn ratios of the ideal transformers in the model are equal $\left(N_{1}=N_{2}\right)$, regardless of $i_{L l k}$ shape, we always have $i_{V L}=i_{L M 1}+i_{L M 2}$. On the other hand, if the shape of $i_{L M 1}$ and $i_{L M 2}$ are the same with a phase-shift of $180^{\circ}$, the LVS-current-ripple cancellation is feasible. For this purpose, the main switches in each operation mode should be driven with the interleaved pattern in which a phase-shift of $180^{\circ}$ is applied between them. Besides, in the ideal case, the operating duty cycles of both phases, the average values of phases current and each phase's specifications should be the same. The simplified waveforms of $i_{L M 1}, i_{L M 2}$ and $i_{V L}$ shown in Fig. 6 are clarified the mentioned points. Hence, if the mentioned conditions is satisfied, regardless of converter operation mode, output power, and the voltage levels of LVS or HVS, the current ripple cancellation would be obtained. From Fig. 6, the current-ripple of the LVS current ( $\Delta i_{V L}$ ) would be derived as:

$$
\begin{equation*}
\Delta i_{V L}=\frac{2 V_{L}(D-0.5)}{L_{M} f} \tag{28}
\end{equation*}
$$

where, $f$ is the operating switching frequency of the converter. Also, the current-ripple ratio of LVS current ( $i_{V L}$ ) to magnetizing inductor current $\left(i_{L M}\right)$ is obtained as:

$$
\begin{equation*}
\frac{\Delta i_{V L}}{\Delta i_{L M}}=\frac{2(D-0.5)}{D} \tag{29}
\end{equation*}
$$

From (28) and (29), the normalized value of $\Delta i_{V L}$ versus duty-cycle, and $\Delta i_{V L} / \Delta i_{L M}$ versus duty-cycle are depicted in Fig. 8.

## IV. DESIGN CONSIDERATIONS

This section describes various design parameters of the proposed converter. For this purpose, the initial points that should be considered are as follows:

- Since the voltage waveforms of $L_{M 1}$ and $L_{M 2}$ include two similar waveforms with a phase-shift of $180^{\circ}$, to realize the current-ripple-cancellation, the values of the magnetizing inductors $L_{M 1}$ and $L_{M 2}$ should be equal $\left(L_{M 1}=L_{M 2}=L_{M}\right)$.
- The average values of $i_{L M 1}$ and $i_{L M 2}$ are equal ( $I_{L M}$ ). In fact, the current-balance between the two phases is established.
- As discussed in the previous section, to realize the current-ripple-cancellation, the turn ratios of the ideal transformers in the model should be selected the same $\left(N_{1}=N_{2}=N\right)$.
- Due to similar condition of the LVS switches ( $S_{1}$ and $S_{2}$ ), the values of their snubber capacitors can be selected the same $\left(C_{S 1}=C_{S 2}=C_{S L}\right)$. Similarly, since the conditions of the HVS switches ( $S_{3}$ and $S_{4}$ ) are almost the same, the values of their snubber capacitors are selected equally $\left(C_{S 3}=C_{S 4}=C_{S H}\right)$.


Fig. 8. (a) Normalized value of LVS current ripple ( $\Delta i_{V L}$ ) versus duty-cycle. (b) Current-ripple ratio of LVS current $\left(i_{V L}\right)$ to magnetizing inductor current ( $i_{L M}$ ) versus duty-cycle.

## A. ZVS Condition

To guarantee the ZVS condition of the proposed converter in boost mode, at the beginning of intervals 6 and 12, the stored energy in $L_{M 1}$ and $L_{M 2}$ should be sufficient to discharge $C_{S 1}$ and $C_{S 3}$ from $V_{C}$ to zero, and to charge $C_{S 2}$ and $C_{S 4}$ from zero to $V_{H} / 2$. Similarly, in buck mode, at the beginning of intervals 2 and 8, the sufficient energy should be stored in $L_{M 1}$ and $L_{M 2}$ to discharge $C_{S 2}$ and $C_{S 4}$ from $V_{H} / 2$ to zero, and charge $C_{S 1}$ and $C_{S 1}$ from zero to $V_{C}$. Considering the simplified waveforms of $i_{L M 1}$ and $i_{L M 2}$ in Fig. 6, the current values of $L_{M 1}$ and $L_{M 2}$ at the beginning of intervals 6 and 12 correspond with the negative peak value of $i_{L M 1}$ and $i_{L M 2}$ $\left(-I_{L M, P^{-}}\right)$. Consequently, the ZVS condition in the proposed converter would be written as follows:

$$
\begin{equation*}
\frac{1}{2} L_{M}\left(-I_{L M, P}^{-}\right)^{2}>\frac{1}{2} C_{S L} V_{C}^{2}+\frac{1}{2} C_{S H}\left(\frac{V_{H}}{2}\right)^{2} \tag{30}
\end{equation*}
$$

It worths mentioning that the ZVS condition of (30) is also valid in buck mode since the current values of $L_{M 1}$ and $L_{M 2}$ at the beginning of intervals 2 and 8 of buck mode also correspond with the negative peak value of $i_{L M 1}$ and $i_{L M 2}$ $\left(-I_{L M, P}^{-}\right)$.

By substituting $V_{C}$ from (25) in (30), and by considering an additional $50 \%$ margin for the tolerances of the devices and losses of parasitics elements, the ZVS condition in both the boost and buck operation modes would be derived as

$$
\begin{equation*}
-I_{L M, P}^{-}<-\frac{1.5 V_{H}}{2} \sqrt{\frac{1}{L_{M}}\left(C_{S H}+\frac{C_{S L}}{(N+1)^{2}}\right)} \tag{31}
\end{equation*}
$$

It worths mentioning that the value of $L_{M 1}$ and $L_{M 2}\left(L_{M}\right)$ determines the value of $-I_{L M, P}{ }^{-}$based on the operating condition of the converter, which is discussed in Subsection C.

## B. Selection of Snubber Capacitors

The snubber capacitors are responsible for the reduction of switches turn-OFF losses. It should be noted that using the larger values for the snubber capacitors causes the reduction of the switches turn-OFF losses. However, as (31) shows, when the values of snubber capacitors ( $C_{S L}$ and $C_{S H}$ ) are selected large, the required value of $-I_{L M, P^{-}}$, and so, the current ripple of $i_{L M 1}$ and $i_{L M 2}$ would be increased. This issue causes increased conduction and core losses. Hence, in the proposed converter, the selecting the minimum values for the snubber capacitors is desirable.

## C. Design of $L_{M 1}$ and $L_{M 2}$ to Obtain ZVS Condition

The value of magnetizing inductors $L_{M 1}$ and $L_{M 2}\left(L_{M}\right)$ determines the current ripple of $i_{L M}$, and so the value of $-I_{L M, P}{ }^{-}$. Hence, the value of $L_{M}$ has an important role in providing ZVS condition in (31). To ensure the ZVS condition (31) in the entire operating range, the value of $L_{M}$ should be selected at the worst-case operating point, when, the average value of $i_{L M 1}$ and $i_{L M 2}\left(I_{L M}\right)$ has the maximum value $\left(I_{L M, \max }\right)$. In this operating point, $i_{L M 1}$ and $i_{L M 2}$ has the maximum level and the value of $\left|-I_{L M, P}{ }^{-}\right|$is minimized. Hence, if the value of $L_{M}$ is designed for this operating point, in the other operating points where the value of $I_{L M}$ is reduced, the value of $\left|-I_{L M, P}{ }^{-}\right|$is increased, and the ZVS condition of (31) would be satisfied. As a result, the ZVS condition is obtained for the entire operating range of the converter.

In the proposed converter, since $i_{V L}=i_{L M 1}+i_{L M 2}$, $I_{V L}=P_{o} / V_{L}$, and $I_{L M 1}=I_{L M 2}=I_{L M}$, the average value of $i_{L M}\left(I_{L M}\right)$ would be equal to $P_{o} / 2 V_{L}$. Hence, the value of $I_{L M}$ is maximized when the converter operates in maximum output power $\left(P_{o, \max }\right)$ and $V_{L}$ has the minimum value $\left(V_{L, \min }\right)$. Consequently, the maximum average value of $i_{L M 1}$ and $i_{L M 2}$ ( $I_{L M, \max }$ ) would be obtained as:

$$
\begin{equation*}
I_{L M, \max }=\frac{P_{o, \max }}{2 V_{L, \min }} \tag{32}
\end{equation*}
$$

Fig. 9(a) illustrates the simplified waveform of $i_{L M 1}$ at operating point that the average value has the maximum value (worst-case condition). In Fig. 9(a), to simplify the analysis, the value of $\Delta i_{L M}$ is considered $2(1+\beta) I_{L M, \max }$. Hence, the value of the negative peak would be $-\beta I_{L M, \max }$. From Fig. 9(a), the value of $L_{M}$ is

$$
\begin{equation*}
L_{M}=\frac{V_{L, \min } D_{\max }}{2 f_{\min }(1+\beta) I_{L M, \max }} \tag{33}
\end{equation*}
$$

where, $f_{\min }$ is the minimum switching frequency, and the value of $I_{L M, \text { max }}$ is obtained from (32). It worths mentioning that $f_{\text {min }}$ is considered when the converter operates with variable frequency control. The variable frequency control is discussed in the next subsection. If the converter operates with the


Fig. 9. (a) Simplified waveform of $i_{L M 1}$ when its average value ( $I_{L M}$ ) has maximum value. (b) Design process of $L_{M}$ value.
constant switching operation, the switching frequency should be considered for $f_{\min }$. Besides, $D_{\max }$ is the maximum value of duty cycle in boost mode. From (23), the value of $D_{\text {max }}$ is derived as:

$$
\begin{equation*}
D_{\max }=1-\frac{2 V_{L, \min }(1+N)}{V_{H, \max }} \tag{34}
\end{equation*}
$$

Now, to design of $L_{M}$ from (33), it is important to select the value of $\beta$, such that the value of $-I_{L M, P}{ }^{-}$is large enough to satisfy ZVS condition in (31). Since $-I_{L M, P}{ }^{-}=-\beta I_{L M, \max }$, if $\beta>0$, the value of $-I_{L M, P^{-}}$would be in the negative region. By a proper over design, the initial value of $\beta$ can be selected equal to one, and so, the values of $-I_{L M, P}{ }^{-}$ and $\Delta i_{L M}$ would be $-I_{L M, \max }$ and $2 I_{L M, \max }$, receptively. Based on these values and the converter specifications, the ZVS condition in (31) is checked. If the ZVS condition is satisfied, the design of $L_{M}$ value is finished. Otherwise, the value of $\beta$ should be selected larger ( $\beta=\beta+0.5$ ), and the design procedure of $L_{M}$ value is repeated. Fig. 9(b) illustrates the design process of $L_{M}$ value, as discussed above. Note that the discussed design procedure of $L_{M}$ is valid in both boost and buck operation modes.

(a)

(b)

(c)

Fig. 10. (a) Waveform of $i_{L M 1}$ at the operating point that $I_{L M}<I_{L M, \max }$ and $-I_{L M, P^{-}}=-\beta I_{L M, \max }$. (b) Values of $f / f_{\min }$ versus $I_{L M} / I_{L M, \max }$ for a specific values of $V_{L}$ and $V_{H}$. (c) Overall block diagram of the control circuit.

## D. Variable Frequency Control

Generally, in TCM operation, to achieve the ZVS condition and reverse recovery cancellation, the main inductors are designed such that their currents flow in both direction. When the converter operates at a constant switching frequency, the current ripple of main inductors is almost constant for different operating conditions. This issue results in almost constant conduction and core losses, which drops the light loads' efficiency. To alleviate this problem, the variable frequency control (VFC) can be applied such that when the output power is reduced, the switching frequency is increased to reduce the current ripple of main inductors.

In the selection of the switching frequency in proportion to the output power, as discussed in subsection C , it should be noted that the negative value of $i_{L M 1}$ and $i_{L M 2}\left(-I_{L M, P}{ }^{-}\right)$ must always be at the desired level to satisfy the ZVS condition $\left(-I_{L M, P}{ }^{-}=-\beta I_{L M, \max }\right)$.

Fig. 10(a) illustrates the waveform of $i_{L M 1}$ at the operating point that its average value is lower than maximum value $\left(I_{L M}<I_{L M, \max }\right)$. Also, its negative value is at the level
of $-\beta I_{L M, \text { max }}$, which satisfies the ZVS condition. From Fig. $10(\mathrm{a})$, considering that $f=1 / T=1 /\left(T_{\mathrm{ON}}+T_{\mathrm{OFF}}\right)$, and from (25), the value of switching frequency $f$ corresponds to this operating point would be

$$
\begin{equation*}
f=\frac{V_{L}\left(V_{H}-2 V_{L}(N+1)\right)}{2 L_{M} V_{H}\left(I_{L M}+\beta I_{L M, \max }\right)} . \tag{35}
\end{equation*}
$$

From (35), and based on measured values of $V_{H}, V_{L}$, and $I_{L M}$, the value of switching frequency can be calculated. Based on (35), and for a specific values of $V_{L}$ and $V_{H}$, the values of $f / f_{\min }$ versus $I_{L M} / I_{L M, \max }$ are depicted in Fig. 10(b).

To reduce the variables that need to be measured from the converter, and by substituting $V_{L}$ or $V_{H}$ from (23) in (35), the value of switching frequency $f$ can be calculated from

$$
\begin{equation*}
f=\frac{V_{H}(1-D)}{4 L_{M}(1+N)\left(I_{L M}+\beta I_{L M, \max }\right)} \tag{36}
\end{equation*}
$$

or,

$$
\begin{equation*}
f=\frac{V_{L} D}{2 L_{M}\left(I_{L M}+\beta I_{L M, \max }\right)}, \tag{37}
\end{equation*}
$$

where, in (36), the variables that need to be measured from the converter include $I_{L M}$ and $V_{H}$. Also, the equation (37) requires $I_{L M}$ and $V_{L}$. It worths mentioning that the equations (35), (36), and (37) are valid in both boost and buck operation modes.

Fig. 10(c) illustrates the overall block diagram of the control circuit based on the calculation of $f$ from (37). The average current mode control can be utilized for each phase to control the current and obtain the current balancing between phases. The value of $I_{L, \text { ref }}$ is determined from an outer control unit, based on the condition and requirements of the system.

In the proposed converter, the values of $i_{L 1}$ and $i_{L 2}$ are equal to $i_{L M 1}-N i_{L l k}$ and $i_{L M 2}+N i_{L l k}$, respectively (See Fig. 1(b)). Since the average value of $i_{L l k}$ is equal to zero $\left(I_{L l k}=0\right)$, the equations of $I_{L 1}=I_{L M 1}$ and $I_{L 2}=I_{L M 2}$ are established. Assuming that the current balancing between phases is established, we have $I_{L 1}=I_{L 2}=I_{L M}$. Hence, the measured value of $I_{L 1}$ (or $I_{L 2}$ ) would be equal to $I_{L M}$.

It worths mentioning that to implement the VFC unit, as illustrated in Fig. 10(c), an additional processor is required to calculate the corresponding switching frequency. This way, compared to constant switching operation, the switching losses at light loads are reduced, resulting in improved efficiency at light loads. On the other hand, to implement the control unit in constant switching frequency, the frequency calculation unit is eliminated, and only the sawtooth wave with constant switching can be applied. Hence, in constant frequency operation, the converter control would be more simple, albeit with the cost of reduced efficiency.

## V. Experimental Results

To verify the theoretical analysis, a prototype of the proposed converter is implemented. Table I presents the prototype specifications and values/part numbers of the components.

TABLE I
PROTOTYPE SPECIFICATIONS AND VALUES/PART NUMBERS OF UTILIZED COMPONENTS.

| Symbol | Parameter | Value/Part Number |
| :---: | :---: | :---: |
| $P_{o}$ | Output Power | 400 W |
| $V_{H}$ | HVS Voltage | 400 V |
| $V_{L}$ | LVS Voltage | 48 V |
| $f_{\min }$ | Minimum Switching Frequency | 100 kHz |
| $S_{1}, S_{2}$ | LVS Switches | IRF200P223 |
|  |  | $(200 \mathrm{~V} / 100 \mathrm{~A})$ |
| $S_{3}, S_{4}$ | HVS Switches | IPW65R041CFD |
| - | Magnetic Cores | $(650 \mathrm{~V} / 68.5 \mathrm{~A})$ |
| $L_{M}$ | Magnetizing Inductance | $17.3 \mu \mathrm{H} / \mathrm{H}$ |
| $N$ | Turn Ratio | 0.68110 A 2 |
| $L_{l k}$ | Equivalent Leakage Inductance | $2.8 \mu \mathrm{H}$ |
| $C_{C}$ | Clamp Capacitor | MKT1820547165 |
|  |  | $(4.7 \mu \mathrm{~F} / 160 \mathrm{~V})$ |
| $C_{H 1}, C_{H 2}$ | HVS Capacitors | B32526R3686K000 |



Fig. 11. Operating frequency $(f)$ of the prototype converter versus output power $\left(P_{o}\right)$ in the variable frequency operation.

## A. Design Procedure

Based on the values of $V_{L}$ and $V_{H}$, considering the operating duty cycle of 0.6 in the boost mode ( $D=0.6$ ), from (23), the value of turn ratio $(N)$ is obtained 0.67. From (25), the voltage stress of $S_{1}$ and $S_{2}$ is 120 V . Also, the voltage stress of $S_{3}$ is $400 \mathrm{~V}\left(V_{H}\right)$, and from (26), the voltage stress of $S_{4}$ would be 280 V . For $S_{1}$ and $S_{2}$, IRF200P223 $\left(V_{\mathrm{DS}}=200 \mathrm{~V}, R_{\mathrm{DS}(\mathrm{ON})}=9.5 \mathrm{~m} \Omega, C_{\mathrm{oss}}=\right.$ 628 pF ) is utilized. Also, IPW65R041CFD ( $V_{\mathrm{DS}}=650 \mathrm{~V}$, $\left.R_{\mathrm{DS}(\mathrm{ON})}=37 \mathrm{~m} \Omega, C_{\mathrm{oss}}=400 \mathrm{pF}\right)$ is used for $S_{3}$ and $S_{4}$. The output capacitors of switches are utilized as the snubber capacitors. Hence, we have $C_{S 1}=C_{S 2}=C_{S L}=628 \mathrm{pF}$ and $C_{S 3}=C_{S 4}=C_{S H}=400 \mathrm{pF}$.

To select the inductance value of $L_{M}$, based on the design process in Fig. 9(b), values of $I_{L M, \text { max }}$ and $D_{\text {max }}$ are obtained 4.17 A and 0.6 , respectively. Moreover, from Fig. 9(b) and considering $\beta=1$, the values of $\Delta i_{L M},-I_{L M, P}{ }^{-}$and $L_{M}$ would be obtained $16.7 \mathrm{~A},-4.17 \mathrm{~A}$ and $17.3 \mu \mathrm{H}$, respectively. Finally, from ZVS condition, the valid equation of $-4.17 \mathrm{~A}<$ -1.80 A would be obtained. Hence, the design process is

(a)

(b)

Fig. 12. Experimental waveforms (time scale is $4 \mu \mathrm{~S} / \mathrm{div}$ ) at full-load ( 400 W ) ( $f=100 \mathrm{kHz}$ ) in (a) boost mode. (b) buck mode.


Fig. 13. Experimental waveforms (time scale is $4 \mu \mathrm{~S} / \mathrm{div})$ at $25 \%$ of full-load ( 100 W ) ( $f=100 \mathrm{kHz}$ ) under constant frequency operation in (a) boost mode. (b) buck mode.
finished with the obtained values. For the magnetic cores, high flux toroid C058110A2 ( $V_{e}=20.7 \mathrm{~cm}^{3}, A_{e}=144 \mathrm{~mm}^{2}$ ) is utilized. The number of windings turns of the primary and secondary sides is 15 and 11 , respectively.

Based on the converter specifications, the voltage of capacitors $C_{H 1}$ and $C_{H 2}$ is $200 \mathrm{~V}\left(V_{H} / 2\right)$, and the voltage of clamp capacitor ( $V_{C}$ ) would be 120 V . For the capacitors $C_{H 1}$ and $C_{H 2}$, Film Capacitor B32526R3686K000 ( $68 \mu \mathrm{~F} / 250 \mathrm{~V}$ ) is utilized. Also, Film Capacitor MKT1820547165 (4.7 $\mu \mathrm{F} / 160$ V ) is applied for the clamp capacitor $C_{C}$.

Finally, to implement the variable frequency control for improving the efficiency at light loads, based on the operating condition and parameters of the converter, the operating switching frequency is calculated from (37). For the operating point of $V_{L}=48 \mathrm{~V}$ and $V_{H}=400 \mathrm{~V}$, the operating frequency of the prototype converter versus output power $\left(P_{o}\right)$ in the variable frequency operation is depicted in Fig. 11.

## B. Experimental Waveforms

Here, the prototype converter's experimental waveforms are presented. Fig. 12 shows the proposed converter's experimental waveforms at full-load condition ( 400 W ). Moreover, the experimental waveforms at $25 \%$ of full load $(100 \mathrm{~W})$ with constant frequency operation ( 100 kHz ) are shown in Fig. 13. It worths mentioning that in both constant frequency operation and variable frequency control, the converter operates with the switching frequency of 100 kHz at the full-load condition.

As seen in Figs. 12 and 13, the experimental waveforms are in accordance with the theoretical analysis, including all the switches voltage stresses. The main switches' waveforms clearly show the ZVS condition as their voltages drop to zero completely before the main switches' turn-ON instants. As observed from the synchronous switches' current waveforms, the current direction is changed through the switch before the switch's turn-OFF instant. Hence, the synchronous switches’


Fig. 14. Experimental waveforms (time scale is $4 \mu \mathrm{~S} / \mathrm{div}$ ) at $25 \%$ of full-load ( 100 W ) ( $f=160 \mathrm{kHz}$ ) under variable frequency control in (a) boost mode. (b) buck mode.


Fig. 15. Prototype's loss breakdown at different output power conditions under (a) Constant frequency operation. (b) Variable frequency control.
body diodes do not conduct in this region, and the reverse recovery losses of the synchronous switches body diodes are eliminated. According to current waveforms of LVS ( $i_{V L}$ in boost mode and $-i_{V L}$ in buck mode), the LVS current benefits from the continuous-non-pulsating state.


Note: The losses of utilized laboratory circuits for control and gate drive are included.

Fig. 16. Calculated and measured efficiency curves of the prototype converter versus output power under constant frequency operation and variable frequency control.

Fig. 14 shows the experimental waveforms of the proposed converter at $25 \%$ of full load ( 100 W ) under variable frequency control. According to Fig. 11, in the prototype converter, when the output power $\left(P_{o}\right)$ is 100 W , the switching frequency would be equal to 160 kHz . As seen in Fig. 14, the proposed converter features, including voltage stresses, ZVS, elimination of diode reverse recovery, and continuous-non-pulsating state of LVS current, are still well established. Besides, compared to the experimental waveforms of 100 W under the constant switching frequency of 100 kHz shown Fig. 13, the current-ripples of the magnetic elements as well as switches are reduced significantly. This feature causes reduced conduction losses and core losses, which is clarified in the next subsection.

## C. Power Losses Analysis and Comparison

Fig. 15 presents the prototype's loss breakdown at different output power conditions under constant frequency operation

TABLE II Comparison between the Proposed Converter and Previous Counterpart Converters．

|  |  |  |  |  |  |  | U 合気 苟 a |  | U 耧 을 on |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No．of Switches | 6 | 5 | 4 | 4 | 4 | 4 | 4 | 4 | 4 | 4 |
| No．of Mag．Cores | 3 | 1 | 1 | 1 | 3 | 1 | 2 | 3 | 1 | 2 |
| No．of Capacitors | 3 | 3 | 2 | 3 | 5 | 3 | 3 | 4 | 3 | 3 |
| LVS Cur．Ripple | Very Low | Low | High | High | Very Low | High | Low | Very Low | High | Low |
| Continuous LVS Cur． | Yes | No | No | No | Yes | No | Yes | Yes | No | Yes |
| Switching Cond． | ZVS | ZVS | ZVS | ZVS | Hard | ZVS | ZVS | ZCS | ZVS | ZVS |
| Prototype Peak Power | 500 W | 200 W | 300 W | 200 W | 400 W | 1 kW | 1 kW | 600 W | 400 W | 400 W |
| Exp．Peak Eff． | 97．1\％ | 97．3\％ | 96．4\％ | 96．8\％ | 94．2\％ | 96\％ | 95．8\％ | Not Reported | 96．5\％ | $96.6 \%{ }^{1}$ |
| Design Scalability | No | No | No | No | No | No | No | No | Yes | No |
| Control Approach | Volt．Matching Control | Not Reported | Voltage－Mode Control | Not Reported | Voltage－Mode Control | Volt．Matching Control | PWM－PPS <br> Control | Current－Mode Control | PWM－PPS <br> Control | Current－Mode Control ${ }^{2}$ |
| Volt．Stress of LVS Switches ${ }^{3}$ | $\frac{V_{H}}{2 N+1}$ | $\frac{V_{H}}{1+N(2-D)}$ | $\frac{V_{H}}{N+2}$ | $\frac{V_{H}}{N+2}$ | $\frac{V_{H}}{N+2}$ | $\frac{V_{H}}{N+1}$ | $\frac{V_{H}}{N+1}$ | $\frac{V_{H}}{N(N+1)+1}$ | $\frac{V_{H}}{N+2}$ | $\frac{V_{H}}{2(1+N)}$ |
| Volt．Stress of HVS Switches ${ }^{3}$ | $\frac{N V_{H}}{2 N+1}$ | $\frac{N V_{H}}{1+N(2-D)}$ | $\frac{(N+1) V_{H}}{N+2}$ | $\frac{(N+1) V_{H}}{N+2}$ | $\frac{(N+1) V_{H}}{N+2}$ | $\frac{N V_{H}}{N+1}$ | $\frac{N V_{H}}{N+1}$ | $\frac{(1+2 N(1+N)) V_{H}}{N+1}$ | $\frac{(N+1) V_{H}}{N+2}$ | $V_{H}, \frac{(2 N+1) V_{H}}{2(N+1)}$ |
| Voltage Gain ${ }^{3}$ | $\frac{2 N+1}{1-D}$ | $\frac{1+N(2-D)}{1-D}$ | $\frac{N+2}{1-D}$ | $\frac{N+2}{1-D}$ | $\frac{N+2}{1-D}$ | $\frac{N+1}{1-D}$ | $\frac{N+1}{1-D}$ | $\frac{N(N+1)+1}{1-D}$ | $\frac{N+2}{1-D}$ | $\frac{2(1+N)}{1-D}$ |

${ }^{1}$ The losses of utilized circuits for control and gate drive are ignored．
${ }^{2}$ In both constant frequency operation and variable frequency control．
${ }^{3}$ In boost mode（ $D$ is the converter duty－cycle in boost mode）and in the ideal case（ $k=1$ ）．
and variable frequency control．
The conduction losses of the switches and windings are calculated from $R_{\mathrm{DS}(\text { on })} I_{\mathrm{RMS}, \mathrm{Switch}}^{2}$ and $R_{\mathrm{DC}, \text { Coil }} I_{\mathrm{RMS}, \text { Coil }}^{2}$ ， respectively，where the currents＇RMS values have been measured from the experimental waveforms．Based on the specifications of the selected switches and at the junction temperature $\left(T_{j}\right)$ of $75^{\circ} \mathrm{C}, R_{\mathrm{DS}(\mathrm{ON})}$ for the LVS switches $S_{1}$ and $S_{2}$ is $14 \mathrm{~m} \Omega$ ，and for the HVS switches $S_{3}$ and $S_{4}$ is $56 \mathrm{~m} \Omega$ ．Also，$R_{\mathrm{DC}, \text { Coil }}$ for the primary and secondary windings of the coupled inductors are $18 \mathrm{~m} \Omega$ and $13 \mathrm{~m} \Omega$ ， respectively．It is worth mentioning that the conduction losses of the converter capacitors $C_{H 1}, C_{H 2}$ and $C_{C}$ are calculated from $R_{\mathrm{ESR}} I_{\mathrm{RMS}, \mathrm{Cap}}^{2}$ ，where $R_{\mathrm{ESR}}$ is the equivalent series resistance of the capacitors．Due to low values of $R_{\text {ESR }}$ of the capacitors，the calculated values of capacitors＇conduction losses are obtained below 50 mW ．Hence，the capacitors＇ conduction losses are neglected in loss analysis．

The clamp circuit losses include the conduction losses of diodes $D_{C 1}, D_{C 2}$ and $D_{C 3}$ that is calculated from $V_{D, \mathrm{ON}} I_{\mathrm{avg}, D}$ ．Based on the specifications of the selected diodes and at the junction temperature $\left(T_{j}\right)$ of $75^{\circ} \mathrm{C}, V_{D, \mathrm{ON}}$ is considered equal to 1 V ．Moreover，the currents＇average values have been measured from the experimental waveforms．

The core losses are obtained from the manufacturer＇s core loss density curves．According to the manufacture information， the curves of core loss density are theoretically obtained from Steinmetz equation $P_{C}=a B^{b} f^{c}$ ，where $P_{C}$ is the core loss density in $\mathrm{mW} / \mathrm{cm}^{3}, B$ is the peak flux density in Tesla（T）， and $f$ is the switching frequency in kilohertz $(\mathrm{kHz})$ ．Besides， $a, b$ ，and $c$ are the Steinmetz coefficient provided by the manufacturer．For the selected core，the Steinmetz coefficients are $a=246.54, b=2.218$ ，and $c=1.311$ ．In the end， a constant loss of 3 W is considered as＂other losses＂for the losses of the control and gate drive circuits，based on the
utilized laboratory circuits．
As seen in Fig．15，in variable frequency control，compared to constant frequency operation，the conduction losses of the converter have a significant reduction at light loads．The reason is that，in variable frequency control，as the output power is reduced，the switching frequency is increased；hence，the current ripple of the switches and inductors is reduced．It worths mentioning that，based on the theoretical Steinmetz equation $P_{C}=a B^{b} f^{c}$ for calculating the core loss density， when the output power is reduced，the current ripple and the peak flux density $B$ is reduced，but on the other hand，the switching frequency $f$ is increased．Hence，as shown in Fig． 15 ，the core losses in variable frequency control compared to constant frequency operation do not significantly reduce．

Based on the loss breakdown in Fig．15，the calculated efficiency curves of the prototype converter are illustrated in Fig．16．Besides，to confirm the validity of the loss analysis， the measured efficiency curves of the prototype converter are illustrated in Fig．16．As seen，the experimental peak efficiencies of $95.6 \%$ and $95.9 \%$ are respectively obtained for boost and buck modes at full－load（ 400 W ）by considering the losses of utilized circuits for control and gate drive． Furthermore，regardless of control and gate drive circuits losses，the experimental peak efficiencies at full－load in boost and buck modes are obtained $96.3 \%$ and $96.6 \%$ ，respectively．

The key specifications comparison between the proposed converter and previous counterpart converters are presented in Table II．For better comparisons and based on Table II， the curves of the voltage－gains and voltage stresses of the converters versus windings turn ratio $(N)$ for the operating duty cycle of 0.6 in boost mode $(D=0.6)$ are plotted in Fig． 17.

It can be seen that compared to other topologies，the HVS voltage stress of the proposed converter is higher．However，as


Fig. 17. Comparison between the proposed converter and previous counterpart converters in boost mode ( $D=0.6$ ). (a) Voltage-gains. (b) Voltage stresses of LVS switches. (c) Voltage stresses of HVS switches.
seen in the loss analysis, despite using typical switches with high voltage rating for HVS switches, the overall conduction losses are small due to the low current levels of HVS switches. As a result, this drawback has no significant effect on the converter efficiency.

## VI. CONCLUSION

A high step-up/step-down converter is introduced provides features such as bidirectional power-flow ability, excellent
voltage-gain, very low voltage stress of LVS switches, current sharing, current ripple cancellation, zero voltage switching, elimination of diodes reverse recovery, reduced values of inductors and leakage inductors, and simple clamp circuit. The converter's operation in both boost and buck modes was comprehensively discussed. Besides, the converter specifications were presented, including the voltage-gains in both the ideal and non-ideal cases, the voltage stresses of switches in the ideal case, and current ripple cancellation feasibility. The design considerations were presented considering ZVS in the converter's entire operating region. To improve the light-load efficiency, the variable frequency control was investigated, including all the required equations. Finally, to verify the analysis, the experimental results of a $48 \mathrm{~V}-400 \mathrm{~V}, 400$ W prototype converter were presented. Due to the proposed converter's superior voltage-gain, the mentioned voltage conversion was obtained with reasonable duty-cycle of 0.6 (in boost mode) and windings turn ratio of about 0.7 . Moreover, the voltage stress of 120 V was achieved for LVS switches, and the voltage stresses of upper and lower HVS switches were respectively obtained 400 V and 280 V . The prototype converter's experimental waveforms were all matched with the theoretical analysis. The experimental efficiencies of $95.6 \%$ and $95.9 \%$ were obtained for boost and buck modes at fullload ( 400 W ), respectively. Furthermore, regardless of control and gate drive circuits losses, the experimental peak efficiencies at full-load in boost and buck modes were respectively achieved $96.3 \%$ and $96.6 \%$. Besides, the measured efficiencies of variable frequency control compared to constant frequency operation at $25 \%$ of full-load ( 100 W ) show the improvement of $3 \%$ and $2.4 \%$ in boost and buck modes, respectively.

## Appendix A

Here, the parameters of the utilized model for coupledinductors are obtained. From Fig. 18(a), $v_{1}$ and $v_{2}$ are:

$$
\begin{align*}
& v_{1}=L_{1} \frac{d i_{1}}{d t}+k \sqrt{L_{1} L_{2}} \frac{d i_{2}}{d t}  \tag{38}\\
& v_{2}=k \sqrt{L_{1} L_{2}} \frac{d i_{1}}{d t}+L_{2} \frac{d i_{2}}{d t} \tag{39}
\end{align*}
$$

From the equivalent circuit of the coupled inductor in Fig. 18(b), $v_{1}^{*}$ and $v_{2}^{*}$ are:

$$
\begin{gather*}
v_{1}^{*}=L_{M} \frac{d i_{1}^{*}}{d t}+N L_{M} \frac{d i_{2}^{*}}{d t}  \tag{40}\\
v_{2}^{*}=N L_{M} \frac{d i_{1}^{*}}{d t}+\left(L_{l k}+N^{2} L_{M}\right) \frac{d i_{2}^{*}}{d t} \tag{41}
\end{gather*}
$$

From (38), (39), (40), and (41), considering $v_{1}=v_{1}^{*}, v_{2}=v_{2}^{*}$, $i_{1}=i_{1}^{*}$ and $i_{2}=i_{2}^{*}$, the parameters of the equivalent circuit would be:

$$
\begin{gather*}
L_{M}=L_{1}  \tag{42}\\
L_{l k}=\left(1-k^{2}\right) L_{2}  \tag{43}\\
N=k \sqrt{\frac{L_{2}}{L_{1}}} \tag{44}
\end{gather*}
$$



Fig. 18. Equivalent circuit of coupled inductors. (a) Coupled inductors. (b) Equivalent circuit.

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