

# Majority-Based Spin-CMOS Primitives for Approximate Computing

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**Abstract**—Promising for Digital Signal Processing (DSP) applications, approximate computing has been extensively considered to trade off limited accuracy for improvements in other circuit metrics such as area, power and performance. In this paper, approximate arithmetic circuits are proposed by using emerging nanoscale spintronic devices. Leveraging the intrinsic current-mode thresholding operation of spintronic devices, we initially present a hybrid Spin-CMOS majority gate design based on a composite spintronic device structure consisting of magnetic domain wall motion stripe and magnetic tunnel junction. We further propose a compact and energy-efficient accuracy-configurable adder design based on the majority gate. Unlike most previous approximate circuit designs that hardwire a constant degree of approximation, this design is adaptive to the inherent resilience in various applications to different degrees of accuracy. Subsequently, we propose two new approximate compressors for utilization in fast multiplier designs. The device-circuit SPICE simulation shows 34.58% and 66% improvement in power consumption, respectively, for the accurate and approximate modes of the accuracy-configurable adder, compared to the recently reported Domain Wall Motion-based full adder design. In addition, the proposed accuracy-configurable adder and approximate compressors can be efficiently utilized in the Discrete Cosine Transform (DCT) as a widely-used digital image processing algorithm. The results indicate that the DCT and Inverse DCT (IDCT) using the approximate multiplier achieve  $\sim 2x$  energy saving and  $3x$  speed-up compared to an exactly-designed circuit, while achieving comparable quality in its output result.

**Index Terms**—Approximate computing, accuracy-configurable adder, compressor, spintronic, domain wall motion device.

## I. INTRODUCTION

COMMONLY-USED multimedia applications rely on Digital Signal Processing (DSP) blocks as primary components. In such applications, low power design is an imperative requirement. Recently, approximate computing has been widely considered in algorithmic circuit design to overcome the power issue by exploiting the non-brittle perceptual abilities of human beings [1]–[3]. This means that approximate outputs can be interpreted by human senses despite being inexact. This approach may be effective in reducing circuit

complexity while simultaneously addressing the problem of high energy consumption [2], [4], [5].

Various methods have been proposed for designing approximate circuits which can be categorized into two broad methodologies. The first methodology is based on voltage over scaling (VOS) such as algorithmic noise tolerance (ANT) [6] and significance driven computation (SDC) [7] for modifying or limiting the resultant errors. The second methodology approximates fundamental logic functions at the circuit-level such as a variety of approximate adder realizations [1], [8], [9].

As a basic building block in most DSP systems, the multiplier is typically located on the critical path of such systems, so it contributes significantly to the system's total power consumption and propagation delay, which greatly motivates the need for fast multiplier designs. A fast multiplication operation is usually performed in three steps, including partial product (PP) generation, PP reduction using a carry-save adder (CSA) tree and a fast carry propagation adder (CPA) for the final computation of the product [10]. Most specifically, the PP reduction circuit is crucial in determining the design complexity, latency and power consumption of a multiplier. Hence, improving the performance and energy efficiency of the PP reduction circuit using appropriate arithmetic blocks, such as compressors, can directly improve the performance and energy efficiency of a fast multiplier [5], [11]. Basically, using compressors can reduce energy dissipation by decreasing the number of PP stages in a multiplier. Optimized designs of accurate 4-2 compressors have been proposed in [10], [12]. In addition, several approximate compressors have recently been presented in the literature [13], [14].

These approximate compressors have typically been realized using Complementary Metal-Oxide-Semiconductor (CMOS) AND-OR gates that increase the design complexity and XOR gates that increase the overall switching activity. On the other hand, as we approach the physical limit of CMOS devices, an urgent need arises for a potential alternative or complementary computing technology. Among others, spintronic devices [15] have shown significant promise over the past decade because of their non-volatility, zero leakage current, high integration density, low standby power, and Back End of Line fabrication with the CMOS technology [16]. In this context, different accurate and approximate circuit designs have been presented [17]–[20]. Additionally, leveraging majority logic in nanoscale technologies can bring even higher performance and energy efficiency compared to conventional implementations of arithmetic circuits [21]–[24].

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Nevertheless, a limitation of the aforementioned designs is the hardwired degree of approximation within the circuit. Therefore, the circuit can only be adjusted to meet a single quality constraint, limiting the possibility of achieving a different quality level [7], [25]. This drawback limits the circuit's practicality, since a programmable platform could facilitate execution of a range of applications with various approximations. Thus, the degree of approximation remains fluid for different applications. Jain et al. in [25] have proposed effective approaches to the design of quality configurable circuits through logic isolation. In another recent work, four dual-quality 4-2 compressors are presented for use in dynamic accuracy-configurable multipliers [14]. Cai et al. in [26] utilizes MTJ switching behavior as an innovative mechanism to switch between accurate and approximate modes.

Some preliminary results of this work have been published in [27]. In [27], a current mode spin-CMOS majority gate based on spintronic threshold device is designed. In addition, an efficient spin-CMOS accuracy-configurable adder is presented utilizing majority gates operating in two distinct modes (approximation and precision). In this paper, new designs of approximate 4-2 compressors are proposed for efficient implementations in DSP systems. As a significant extension of [27], this manuscript makes the following novel contributions:

- two distinct designs for 4-2 approximate compressors are developed based on presented scalable current mode spin-CMOS majority gate using spintronic threshold device. These designs are further leveraged for implementing fast multiplier design as a basic block in DSP hardware,
- a comprehensive evaluation framework is constructed for the proposed designs from device to application level, and
- both the accuracy-configurable adder and approximate compressors are utilized in image compression, and the resultant output quality and energy trade-offs are assessed with respect to peak signal-to-noise ratio, delay, and energy consumption.

The remainder of the paper is organized as follows. Section II introduces the spintronic threshold device structure and its modeling. Section III addresses the design and evaluation of spin-CMOS majority gate circuit. In Section IV, the majority gate-based accuracy-configurable adder is designed. Section V is dedicated to proposal of highly-efficient and low-cost approximate 4-2 compressors. Section VI discusses circuit level performance evaluation of the proposed designs. Section VII assesses the efficacy of the presented circuits in image processing applications and Section VIII concludes the paper.

## II. SPINTRONIC THRESHOLD DEVICE STRUCTURE

In this section, we present Spintronic Threshold Device (Spin-TD) based on a composite device structure consisting of a Domain Wall Motion (DWM) magnetic stripe and Magnetic Tunnel Junction (MTJ). The device structure for the Spin-TD is shown in Fig. 1a [15], [28]–[31]. It consists of a thin and short ( $2\text{nm} \times 20\text{nm} \times 50\text{nm}$ ) magnetic Domain Wall Stripe (DWS) connecting two fixed anti-parallel magnetic domains. When the electrons are injected into the lateral terminals (T1 or T2), they become spin-polarized and exert a Spin-Transfer

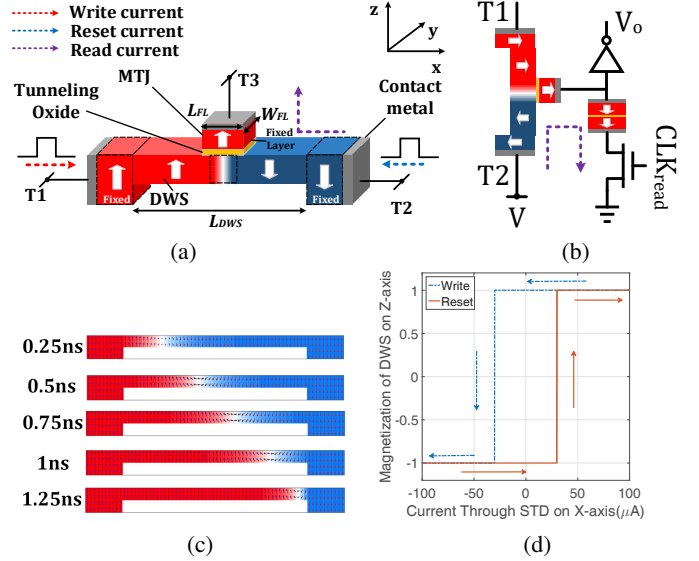


Figure 1. (a) Spintronic threshold device (Spin-TD) structure, (b) Spin-TD sense circuit, (c) Micro-magnetic simulation for the DW position, (d) Spin-TD transfer function and reset.

Torque (STT) on the Domain Wall (DW) (i.e., the transition area between two domains). This spin-polarized current can move DW within DWS. A fixed small magnet and DWS beneath it form a MTJ to read the state of DWS. It is noteworthy that an MTJ [32] consists of two ferromagnetic layers (a free layer and a fixed one as shown in Fig. 1a) with a tunneling oxide (commonly MgO) barrier sandwiched between them [15].

The fixed layer of sense MTJ in Spin-TD is very small ( $20\text{nm} \times 20\text{nm}$ ). The magnetization of DWS can be identified anti-parallel (AP) or parallel (P) to the fixed layer by injecting a current (larger than critical current) along it from its terminals (T1 to T2) or vice-versa [33]. Hence, the Spin-TD can detect the polarity of current flow at its input node, acting as an ultra-low voltage and compact current comparator. The resistance states are binary, i.e. either high (corresponding to AP configuration) or low (corresponding to P configuration) and can be read employing the Spin-TD sense circuit as shown in Fig. 1b). The threshold of Spin-TD, i.e. the minimum current magnitude required to switch the DWS magnetization (move DW from one end to the other end), is determined by the critical current density and DW velocity.

The transient micro-magnetic simulation of DW position (achieved from OOMMF [34]) is illustrated in Fig. 1c, using device dimension shown in Table I, from 0.25 ns to 1.25 ns. Since the magnetization of DWS beneath the MTJ is fully switched at 1ns, the Spin-TD intrinsic threshold ( $I_{th}$ ) of this device can be considered  $30\mu\text{A}$  within 1 ns corresponding to DW velocity of  $\sim 50\text{m/s}$ . Fig. 1d describes DWS magnetization switch corresponding to the applied current pulse (1 ns). A hysteresis effect can be observed due to DWM critical current density. The device parameters used in the simulation are listed in Table I. We benchmarked the micro-magnetic simulation with the experimental data in [35] (the same nano-stripe width of 20nm is fabricated) and it shows a good match as shown in Fig. 2a. The MTJ is modeled using

Table I  
DEVICE PARAMETERS USED IN SIMULATION.

Symbol	Quantity	Values
$\alpha$	Damping coefficient	0.02
$K_u$	Uniaxial anisotropy constant	$3.5 \times 10^5 \text{ J/m}^3$
$M_s$	Saturation magnetization	$6.8 \times 10^5 \text{ A/m}$
$A_{ex}$	Exchange stiffness	$1.1 \times 10^{-11} \text{ J/m}$
$P$	Polarization	0.6
$t_{MgO}$	MgO thickness of MTJ	1.5 nm
$(L.W.t)_{DWS}$	DWS dimension	$50 \times 20 \times 2 \text{ nm}^3$

NEGF-LLG solution (non-equilibrium Green's function and Landau-Lifshitz-Gilbert equations) for spin to charge interface and calibrated with experimental data in [35], [36]. Resistance-area (RA) product vs. the thickness of tunneling oxide in AP and P states in this work considering a constant voltage of 50mV is plotted in Fig. 2b. Basically, the resistance-area (RA) product of the MTJ, which corresponds to the thickness of the MTJ tunneling oxide and the reliability of the MTJ, needs to meet the design specifications. Otherwise an accident write of MTJ may occur when the current flowing through the MTJ, is more than threshold current,  $I_{th}$ , during read operation. It may occur when a thinner  $t_{MgO}$  is used, which further leads to logic failure. Our simulations showed that 1.5nm thickness provides the circuit with a favorable reliability during sensing.

The effective resistance of the MTJ formed between DWS and fixed layer (T3 side) is smaller when they have the identical magnetization and vice versa. The ratio of two resistances is defined in terms of Tunneling Magneto Resistance ratio (TMR). As shown in Fig. 1b, Spin-TD forms a voltage divider with a fixed reference MTJ to sense the resistance state. Static current in the voltage divider can be minimized by increasing the MTJ oxide thickness. For a 1 ns clock cycle, the oxide thickness in this work is chosen to be 1.5 nm that results in a total power dissipation of  $\sim 1\mu W$  for the sensing circuit (including the clocking power). It is worth noting that in the sense circuit, the transient current with short duration (1 ns) and low magnitude ( $\sim 2\mu A$ ) flows from T2 to T3, which will not disturb the state of DWS (domain wall position). The sense current can be further reduced to less than  $1\mu A$  by increasing the oxide thickness [33].

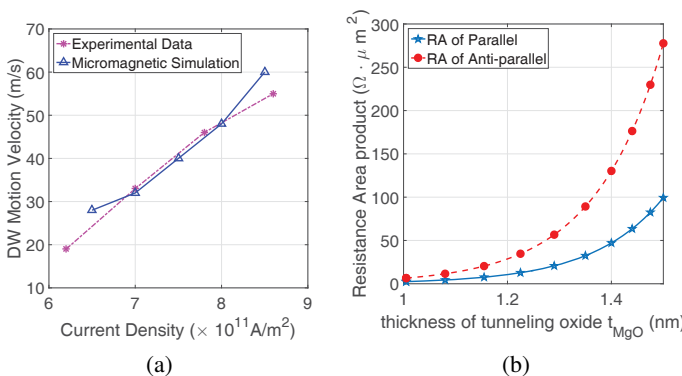


Figure 2. (a) Simulated DW motion velocity vs. lateral current density, showing a good match with experimental data reported in [35], (b) Resistance-area product vs. the thickness of tunneling oxide in AP and P state (with 50mV constant voltage).

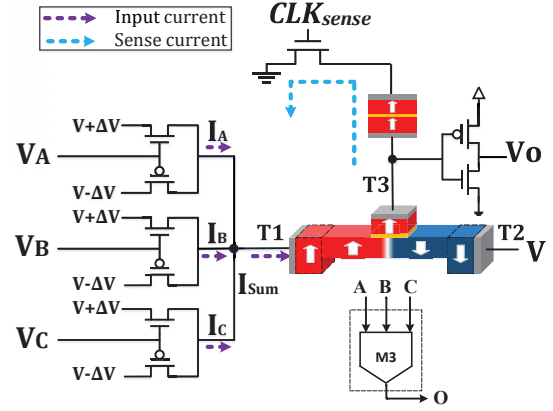


Figure 3. Spin-CMOS implementation of three-input majority gate.

### III. SPIN-CMOS MAJORITY GATE CIRCUIT DESIGN

In this section, we present a highly-scalable spin-CMOS majority gate circuit design based on Spin-TD. The output of an  $n$ -input Majority Gate (MG) ( $n$  is odd) is determined by the majority of its inputs. For instance, the output is asserted to be logic value “1” only when more than  $(\frac{n-1}{2})$  of the inputs are “1”.

The proposed three-input MG circuit employing Spin-TD is shown in Fig. 3. As shown, the input terminal (T1) is connected to a network consisting of 3 pairs of NMOS-PMOS input transistors, in which all of the input transistors work as Deep Triode region Current Sources (DTCS) by applying  $V + \Delta V = 550 \text{ mV}$  and  $V - \Delta V = 450 \text{ mV}$  to the source and drain, respectively. The proposed circuit is controlled by two clock signals ( $CLK_{compute}$  and  $CLK_{sense}$ ) and each clock period is set to be 1 ns to synchronize with next stage circuits (discussed thoroughly in Section VI). Note that, T2 of Spin-TD is connected to a constant voltage of  $V = 500 \text{ mV}$  and the voltage difference is  $\Delta V = 50 \text{ mV}$ , leading to an ultra-small voltage drop and correspondingly-low power consumption.

During the computation clock interval, the binary input voltages (VDD, GND) are applied at the gate of the input transistors, leading to input current flowing into (positive) or out of (negative) the connected Spin-TD. According to the principle of conservation of electric charge, the direction and magnitude of total current at intersection node depend on the algebraic sum of the input currents ( $I_A$ ,  $I_B$  and  $I_C$  herein). This summation current ( $I_{Sum}$ ) determines the position of DW in the DWS as described in Section II. By properly sizing the input transistors, the current flowing to T1 from each input branch is either  $+30\mu A$  or  $-30\mu A$  corresponding to input gate voltages as high (“1”) or low (“0”), respectively. For instance, the input combination of (A, B, C)=(0, 1, 1) leads to  $(I_A, I_B, I_C) = (-30\mu A, +30\mu A, +30\mu A)$  and the total current flowing into T1 is  $+30\mu A$ . Such current is equal to the threshold current of the Spin-TD and relocates the domain wall towards the T1 side, further resulting in the sense MTJ in an anti-parallel high resistance state. During the sense phase, when the  $CLK_{sense}$  is high, a voltage divider between Spin-TD’s MTJ and a fixed reference MTJ is formed to sense the resistance state of spin-CMOS 3-input MG to produce reliable output

Table II  
THREE-INPUT SPIN-CMOS MG CURRENT SUMMATION AT T1 AND  
CORRESPONDING DOMAIN WALL POSITION.

Input Currents ( $\mu A$ )			Summation Current ( $\mu A$ )	Initial DW position		Final DW position
$I_A$	$I_B$	$I_C$	$I_{Sum}$	@Right	@Left	
-30	-30	-30	-90	Right	Right	
-30	-30	+30	-30	Right	Right	
-30	+30	-30	-30	Right	Right	
-30	+30	+30	+30	Left	Left	
+30	-30	-30	-30	Right	Right	
+30	-30	+30	+30	Left	Left	
+30	+30	-30	+30	Left	Left	
+30	+30	+30	+90	Left	Left	

voltage right after the inverter. In this case, the sensing circuit will generate a high output representing logic “1”.

Table II lists eight possible input current combinations and the corresponding summation current. The last two columns of Table II list the DW position before and arrival of the computation clock. It is clear that the proposed 3-input spin-CMOS MG does not require an additional reset clock, since the final DW position is solely determined by the summation current direction and the initial DW position does not have an effect on the final DW position. As an instance, when the  $I_{Sum}$  is equal to or greater than  $+30\mu A$ , either the DW’s initial position is at the right or left side, it will either be pushed towards or remain on the left side. It is worth pointing out that 2-input AND or OR gates can be efficiently designed just by setting one of the three MG inputs to GND or VDD, respectively. In addition, the proposed MG circuit readily allows for the scaling of input fan-in. It means that the 3-input MG circuit design can be effectively extended for implementing  $n$ -bit MGs. To do so, the connected input branches are increased. For instance, a 5-input MG will be obtained by employing five pairs of NMOS-PMOS input transistors without changes in circuit parameters. Note that, in order to produce a highly reliable complementary output voltage, we can also add an additional cascaded inverter to the sensing circuit right after Vo in Fig. 3. In the following two sections, the proposed spin-CMOS MG is used to implement an accuracy-configurable adder and two approximate compressors.

#### IV. SPIN-CMOS ACCURACY-CONFIGURABLE ADDER

##### A. Functionality Analysis

A full adder (FA) is one of the most frequently-used components in arithmetic circuitry. In addition to its regular use for addition, it is employed in other arithmetic operations such as subtraction, multiplication, and division [37]. For instance, multiplication has been implemented using successive additions. Moreover, FA is the key component and optimization target of many DSP algorithms. Hence, in order to obtain a high performance DSP system, we need to design energy efficient and low complexity adders [5]. While extensive work has been done in designing approximate adders [38], [39], the research efforts on accuracy-configurable approximate adders are limited. Let  $A$ ,  $B$  and  $C_{in}$  be inputs of an accurate full adder, the principle Boolean expression of Carry out ( $C_{out}$ ) and accurate Sum ( $Sum_{acc}$ ) of FA cell are as follows:

$$C_{out} = AB + AC_{in} + BC_{in} = M3(A, B, C_{in}) \quad (1)$$

Table III  
TRUTH TABLE FOR ACCURATE AND APPROXIMATE FAS.

Inputs			Acc. Outputs		App. Outputs	
$A$	$B$	$C_{in}$	$C_{out}$	$Sum$	$C_{out}$	$Sum$
0	0	0	0	0	0	✓
0	0	1	0	1	0	✓
0	1	0	0	1	0	✓
0	1	1	1	0	1	✓
1	0	0	0	1	0	✓
1	0	1	1	0	1	✓
1	1	0	1	0	1	✓
1	1	1	1	1	1	✓
1	1	1	1	1	1	✗

$$Sum_{acc} = ABC_{in} + \bar{A}\bar{B}C_{in} + \bar{A}B\bar{C}_{in} + A\bar{B}\bar{C}_{in} \quad (2)$$

Some Boolean expressions for  $Sum_{acc}$  and  $C_{out}$  of FA based on inverters and MGs have been reported in [27], [40], [41]. As can be seen in (1),  $C_{out}$  can be readily derived with a 3-input MG. Alternatively,  $Sum_{acc}$  can be obtained by using 3- and 5-input MG functions as (3).

$$\begin{aligned} Sum_{acc} &= ABC_{in} + (\overline{AB \cdot AC_{in} \cdot BC_{in}})(A + B + C_{in}) \\ &= ABC_{in} + \overline{M3}(A + B + C_{in}) \\ &= ABC_{in} + \overline{M3}(A + B + C_{in}) + \overline{M3}M3 \\ &= M5(A, B, C_{in}, \overline{M3}, \overline{M3}) \\ &= M5(A, B, C_{in}, \overline{C_{out}}, \overline{C_{out}}) \end{aligned} \quad (3)$$

Table III shows the truth table of an FA. A close observation clarifies that six of eight outputs are correct if we make  $Sum = \overline{C_{out}}$ . Based on this observation, we propose a streamlined and cost-effective approximate FA circuit comprising one 3-input MG and one cascaded inverter. The approximate Sum output ( $Sum_{App}$ ) of this adder is given by:

$$Sum_{App} = \overline{C_{out}} = \overline{M3(A, B, C_{in})} \quad (4)$$

##### B. Spin-CMOS Implementation

The proposed spin-CMOS implementation of the accuracy-configurable FA cell is shown in Fig. 4 consisting of two stages: Stage 1 to generate  $C_{out}$  and  $Sum_{app}$  and Stage 2 to generate  $Sum_{acc}$ . The first stage consists of a spin-CMOS MG realizing an approximate FA (App. FA) according to (1) and (4). As shown in Fig. 4, this circuit is designed with an appropriate fan-out for producing  $Sum_{App}$  output after one add-on inverter, while  $C_{out}$  is already achieved according to the Boolean expression in (1).

Meanwhile, the  $\overline{C_{out}}$  (or  $Sum_{app}$ ) produced in Stage 1 is then connected to a similarly scaled input transistor network but with a  $\frac{2w}{l}$  ratio to provide a double weighted current as expressed in (3). The double weighted current in conjunction with the sum of three primary inputs flow towards the T1 of the Stage 2’s MG (realizing a 5-input MG as depicted in the logical schematic in Fig. 4). Consequently, the output voltage of this stage is  $Sum_{acc}$  realizing an accurate FA (Acc. FA). To provide the circuit with a proper and streamlined configurability, the wire connection between these two stages is regulated using a CMOS transmission gate (TG). Furthermore, the sum outputs of both stages are laterally connected to a 2:1 CMOS multiplexer implemented utilizing two TGs to produce

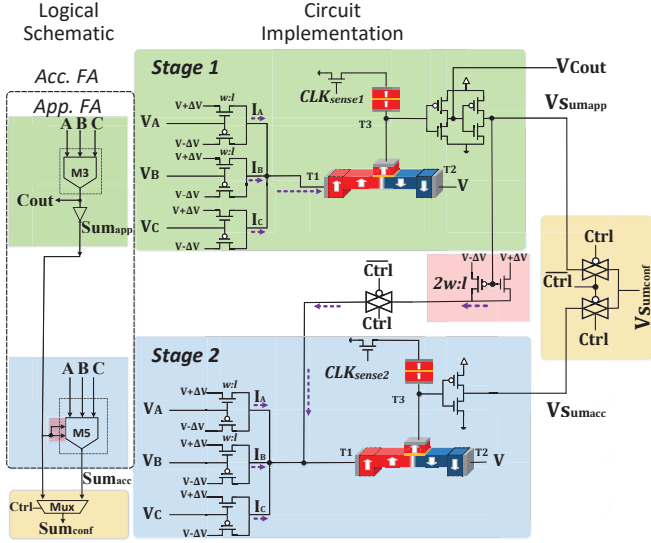


Figure 4. Logical schematic and circuit implementation of Spin-CMOS accuracy-configurable FA. When Ctrl knob is high, the circuit functions as an accurate FA and when Ctrl knob is low, the circuit functions as an approximate adder.

configurable sum ( $Sum_{conf}$ ). Accordingly, the proposed spin-CMOS accuracy-configurable circuit operates in two different modes i.e. precision and approximation. In the precision mode, the control knob ( $Ctrl$ ) is high, so the intermediate TG is ON and the double weighted current is routed to the second stage MG. Consequently, the circuit functions as an accurate adder since the second input of the multiplexer will be transmitted to the output ( $Sum_{conf} = Sum_{acc}$ ). In the approximation mode, the  $Ctrl$  is low and the double weighted branch is disconnected avoiding any switching activity in second stage. Therefore, the Stage 1's circuit works as a low power approximate adder when  $Sum_{conf} = Sum_{app}$ . Timing diagram and analysis are shown later in Fig. 9.

## V. SPIN-CMOS APPROXIMATE COMPRESSORS

A fast multiplier typically consists of three primary modules: (1) a Partial product generator, (2) a Carry save adder (CSA) tree for reducing the partial products, and (3) a Carry propagation adder (CPA) for final computation. The second module dominates the circuit complexity, delay, and power consumption of a multiplier. The main idea behind utilizing multi-operand CSA is to reduce  $n$  numbers to two numbers; that is why  $n - 2$  compressor blocks have been widely explored in computer arithmetic [13], [37]. As shown in Fig. 5a, a widely-used 4-2 compressor receives 4 primary inputs ( $X1 - X4$ ) and one carry bit ( $C_{in}$ ) from the lower position block, then it produces 2 primary outputs ( $Carry$  and  $Sum$ ) and sends one carry bit ( $C_{out}$ ) to the higher position block. Fig. 5b depicts the design of an accurate 4-2 compressor based on the so-called CMOS XOR-XNOR gates [10].

In this section, we propose two designs for approximate 4-2 compressors based on accurate and approximate FAs proposed in Section IV.A. Intuitively, in order to design an approximate 4-2 compressor (with the truth table shown in Table IV), it is possible to replace the accurate full-adder

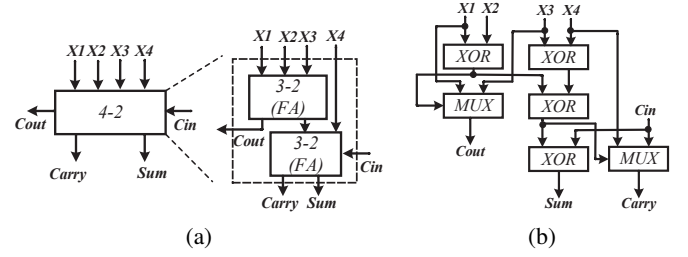


Figure 5. (a) 4-2 compressor using two FAs, (b) Optimized 4-2 compressor [10].

cells by approximate cells. In other words, two cascaded approximate 3-2 compressors can be readily employed to realize an approximate 4-2 compressor (such as the first design presented in [38]). However, this solution has not been very popular so far due to the high error rate of basic modules such that it shows 53% error rate (with at least 17 incorrect results out of 32 possible outputs). Note that herein the error rate is defined as the ratio of number of erroneous outputs to the total number of outputs.

### A. Design I

The gate level structure of the first proposed approximate 4-2 compressor is depicted in Fig. 6a. As can be seen, only two approximate FAs (App. FA) are cascaded to realize such a low-complexity design.  $X1 - X3$  inputs are assigned to the first App. FA and  $X4$ ,  $C_{in}$  along with  $\overline{C_{out}}$  are connected to the second App. FA. In this way,  $C_{out}$  can be obtained accurately for all input combinations using (5).  $Carry'$  is given in (6) with only 4 incorrect outputs as tabulated in Table IV.  $Sum'$  is accordingly derived in (7) by inverting the result of  $Carry'$  with 12 incorrect output out of 32 possible outputs. Overall, Design I yields an error rate of 37.5% that is smaller than the error rate of employing the best approximate FA [38] and the same as that of the first design presented in [13]. Furthermore, Design I shows significant improvement for the critical delay ( $2\Delta^1$ ) compared to the first approximate design in [13] ( $3\Delta$ ) and optimized design in [10] ( $3\Delta$ ).

$$C_{out} = M3(X1, X2, X3) \quad (5)$$

$$Carry' = M3(\overline{C_{out}}, X4, C_{in}) \quad (6)$$

$$Sum' = \overline{Carry'} \quad (7)$$

### B. Design II

Fig. 6b depicts the second proposed design employing one approximate FA (App. FA) and one accurate FA (Acc. FA) cell. Applying an accurate FA cell in the first level ensures that, in addition to  $C_{out}$  (5),  $Carry$  output can be achieved correctly for all input combinations as tabulated in the last few columns in Table IV. This design generates 8 erroneous outputs for  $Sum'$ , therefore the error rate is now reduced to 25%. As a trade-off between accuracy and circuit delay/complexity,



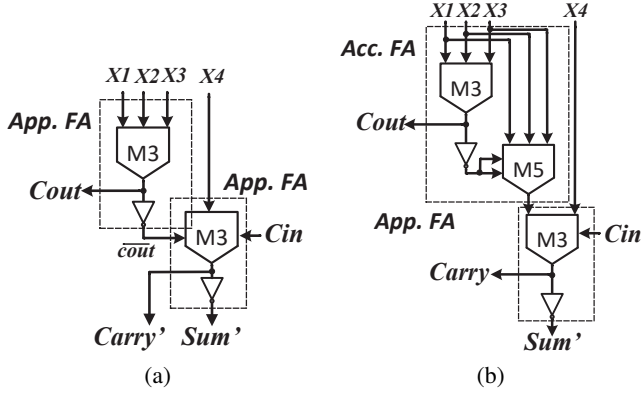


Figure 6. The proposed approximate 4-2 compressors: (a) Design I employs two approximate FAs, (b) Design II employs one accurate and one approximate FA.

Table IV  
TRUTH TABLE FOR ACCURATE AND APPROXIMATE COMPRESSORS.

Inputs					Acc Output			Design I			Design II			
Cin	X <sub>4</sub>	X <sub>3</sub>	X <sub>2</sub>	X <sub>1</sub>	Cout	Carry	Sum	Cout	Carry'	Sum'	Cout	Carry	Sum'	
0	0	0	0	0	0	0	0	0	0	1 $\times$	0	0	1 $\times$	
0	0	0	0	1	0	0	1	0	0	1	0	0	1	
0	0	0	1	0	0	0	1	0	0	1	0	0	1	
0	0	0	1	1	1	0	0	1	0	1 $\times$	1	0	1 $\times$	
0	0	1	0	0	0	0	1	0	0	1	0	0	1	
0	0	1	0	1	1	0	0	1	0	1 $\times$	1	0	1 $\times$	
0	0	1	1	0	1	0	0	1	0	1 $\times$	1	0	1 $\times$	
0	0	1	1	1	1	0	1	1	0	1	1	0	1	
0	1	0	0	0	0	0	1	0	1 $\times$	0 $\times$	0	0	1	
0	1	0	0	1	0	1	0	0	1	0	0	1	0	
0	1	0	1	0	0	1	0	0	1	0	0	1	0	
0	1	0	1	1	1	0	1	1	0	1	1	0	1	
0	1	1	0	0	1	0	1	1	0	1	1	0	1	
0	1	1	0	1	1	0	1	1	0	1	1	0	1	
0	1	1	1	0	1	1	0	1	0 $\times$	1 $\times$	1	1	0	
1	0	0	0	0	0	0	1	0	1 $\times$	0 $\times$	0	0	1	
1	0	0	0	1	0	1	0	0	1	0	0	1	0	
1	0	0	1	0	0	1	0	0	1	0	0	1	0	
1	0	0	1	1	1	0	1	1	0	1	1	0	1	
1	0	1	0	0	0	1	0	0	1	0	0	1	0	
1	0	1	0	1	1	0	1	0	1	0 $\times$	0	1	0 $\times$	
1	0	1	1	0	0	1	1	0	1	0 $\times$	0	1	0 $\times$	
1	0	1	1	1	1	0	1	1	0	1	1	0	1	
1	1	0	0	0	0	1	0	0	1	0	0	1	0	
1	1	0	0	1	0	1	1	0	0	1	0 $\times$	0	1	0 $\times$
1	1	0	1	0	0	1	1	0	1	0 $\times$	0	1	0 $\times$	
1	1	0	1	1	1	1	0	1	1	0	1	1	0	
1	1	1	0	0	0	1	1	0	1	0 $\times$	0	1	0 $\times$	
1	1	1	0	1	1	1	0	1	1	0	1	1	0	
1	1	1	1	0	1	1	1	0	1	0	1	1	0	
1	1	1	1	1	1	1	1	1	0 $\times$	1	1	1	0 $\times$	

design II incurs  $(3\Delta)$  as the critical path delay with an additional 5-input MG compared to design I.

The proposed compressors are readily implemented in hybrid spin-CMOS circuits as shown in the logical diagrams in Fig. 6 based on spin-CMOS MG shown in Fig. 3. Fig. 7 shows Design I implementation by using 2 DWSs and 4 MTJs. Design II is similarly implemented using 3 DWSs and 6 MTJs.

## VI. PERFORMANCE EVALUATION

In order to evaluate the performance of the proposed circuits, we designed a comprehensive simulation framework as shown in Fig. 8. This bottom-up simulation framework can be divided into three main levels:

- 1) Device level: For device level simulation, we benchmarked the domain wall motion dynamics with experimental data [35] utilizing Object Oriented MicroMag-

<sup>1</sup> $\Delta$  is defined as gate delay [13]

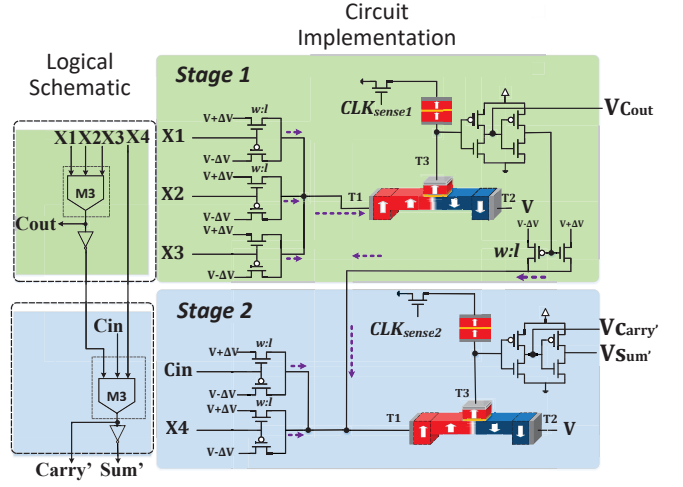


Figure 7. Logical schematic and circuit implementation of Spin-CMOS compressor based on Design I.

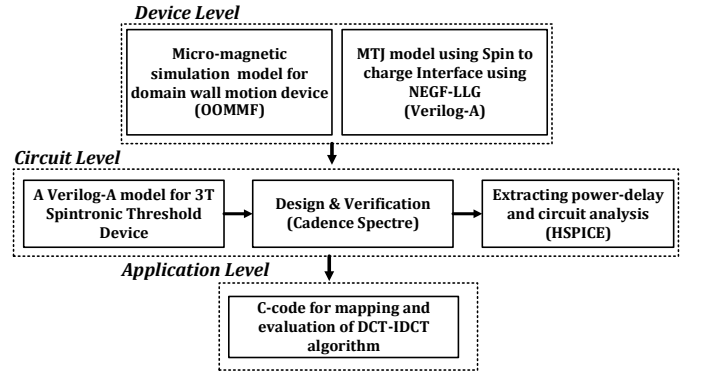


Figure 8. Device to application level co-simulation framework.

netic Framework (OOMMF) [34]. The MTJ (composed of a DWS, a tunneling oxide layer and a fixed ferromagnetic layer) is modeled in Verilog-A, using NEGF-LLG (non-equilibrium Green's function and Landau-Lifshitz-Gilbert equations) solution for spin to charge interface and calibrated with the experimental data in [36].

- 2) Circuit level: For the circuit level simulation, a Verilog-A model of 3T-Spin-TD is developed to co-simulate with the interface CMOS circuits in Cadence Spectre and SPICE. 45nm North Carolina State University (NCSU) Product Development Kit (PDK) library [42] is used in SPICE to verify the proposed design and acquire the performance (power, delay, etc.) of designs.
- 3) Application level: We consider a widely-used image compression algorithm, the Discrete Cosine Transform (DCT), to show the results of using the proposed accuracy-configurable adder and approximate compressor-based multipliers at the application level.

This section deals with device and circuit-level evaluations; however, Section VII is fully dedicated to application level evaluations.

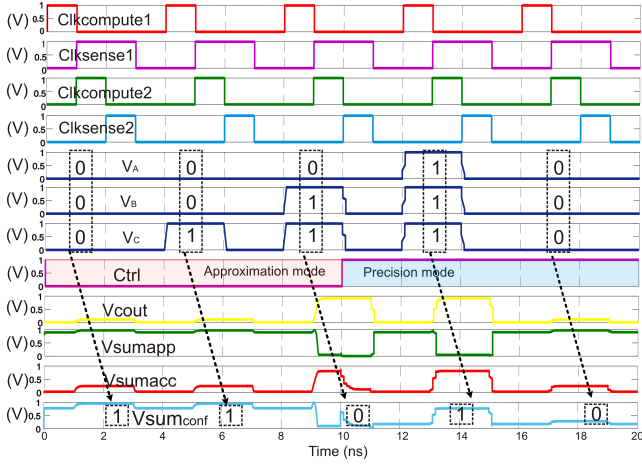


Figure 9. Transient voltage analysis of the proposed accuracy-configurable FA cell.

### A. Accuracy-Configurable Adder

Fig. 9 depicts waveforms of transient voltage analysis of the proposed accuracy-configurable FA cell. A 3 ns period is considered as a full computation cycle for the circuit. Both stages use identical pulse widths of 1 ns for  $CLK_{compute}$ . Stage 1 uses a 2 ns  $CLK_{sense1}$  signal for proper implementation of sensing and Stage 2 uses 1 ns  $CLK_{sense2}$ . Since  $C_{out}$  in Stage 1 is used in the next stage MG, it should last 2 ns to be synchronized with the sum generated in Stage 2. Four input combinations regardless of the sequence (000, 001, 011, and 111) are considered as input vectors (where  $V_A$ ,  $V_B$  and  $V_C$  are A, B, and C voltages, respectively). Moreover,  $V_{Cout}$ ,  $V_{Sum_{app}}$ , and  $V_{Sum_{acc}}$  stand for  $C_{out}$ , approximate sum, and accurate sum voltages, respectively.

In the approximation mode ( $Ctrl=0$ ), when  $Clk_{compute1}$  is high, the input voltages are applied to Stage 1 circuit for 1 ns.  $Clk_{sense1}$  is then activated leading to generate the first stage output voltages ( $V_{Cout}$  and  $V_{Sum_{app}}$ ). As is clear in Fig. 9, for three input combinations of (000, 001, and 011), the final Sum signal  $V_{Sum_{conf}}$  is (1, 1 and 0) corresponding to  $V_{Sum_{app}}$ . It is noteworthy that in the approximation mode, besides switching off the intermediate TGs connecting Stage 1 to Stage 2, power gating is also employed to reduce the power consumption of Stage 2. In the precision mode ( $Ctrl=1$ ), the input voltages are applied to Stage 1 and Stage 2 in two consecutive nanoseconds when  $Clk_{compute1}$  and  $Clk_{compute2}$  are respectively high. After the computation clock of Stage 1,  $Clk_{sense1}$  should be activated for 2 ns in a manner such that the required inputs are fed to the second stage and synchronized outputs are provided for the FA. As is clear in Fig. 9, the valid results can be obtained after applying  $Clk_{sense2}$  so that for two input combinations of (000 and 111), the final Sum signal  $V_{Sum_{conf}}$  is 0 and 1 corresponding to  $V_{Sum_{acc}}$ .

Comparison results between the proposed adder and previously published CMOS- [1], [43], MTJ- [26], [43], Spin Hall Effect (SHE)- [20] and Domain Wall Motion (DWM)- [19] based FAs are summarized in Table V. Various metrics including the device count, total power consumption, and delay are considered for the comparison. In addition, the important approximate computing metric, Error Distance (ED) [44] is

used for approximate adders' evaluation. Basically, in any approximate circuit, the inexact output  $a$  and accurate output  $b$  is compared arithmetically for all possible combination inputs bit by bit:  $ED(a, b) = |a - b| = \left| \sum_i a[i] * 2^i - \sum_j b[j] * 2^j \right|$ , where  $i$  and  $j$  are the indices for the bits in  $a$  and  $b$  [5], [45]. Here, we report Error Rate (ER), Mean Error Distance (MED), as the average of the error distances across all possible input vectors, and Mean Relative Error Distance (MRED) for different designs. The MRED is computed by averaging all possible absolute relative error distances (RED) (i.e.,  $RED = \left| \frac{ED}{b} \right|$ ), where the  $RED$  is not considered when the accurate output  $b$  is 0.

As shown in Table V, the proposed design in approximation mode shows smaller ER, MED and MRED compared to the approximate designs in [26]. However, it shows identical values to the proposed designs in [1], [23]. Since the design proposed in [23] was implemented in NML technology and there was no performance metrics reported in this reference, so the power/delay analysis of the design is inevitably left for future investigations.

Based on Table V, the accuracy-configurable circuit in this work along with the presented designs in [26] are the only adders with the approximation configurability. For a fair comparison, since most of the counterpart designs were designed and evaluated in 180nm, we scaled ours and others to this process node. We have done fixed-voltage scaling by using the appropriate scaling factor, which is  $(1/S^2)$  for area and  $(1/S)$  for energy [46]. In addition, CMOS FAs contain one output register along with FA cell since non-volatile designs also have memory functions.

The results clearly show that the proposed accuracy-configurable adder consumes smaller power than the other designs in [19], [20], [26], [43]. For instance, 34.58% and 66% improvement in power consumption can be reported for the precision and approximation modes, respectively, over the best DWM-based FA design in [19]. In addition, compared to the recently-published work by Roohi et al. in [20], the proposed FA in precision mode can show  $\sim 12.7\times$  and  $2.3\times$  smaller power and delay, respectively.

The area-efficient accuracy-configurable adder also exhibits  $\sim 18\%$  reduction in circuit complexity over the accurate CMOS-based FA design in [43]. However, the proposed design utilizes 28 MOS transistors, which is more than the designs in [1], [19], [26]. It is worth pointing out that the device count can offer a representative estimation of the area overhead since the proposed full adder is more compactly implemented than a CMOS implementation [19], [43].

The proposed adder does not improve delay compared to the previous designs in [1], [19], nonetheless it can achieve higher speed and throughput using pipeline techniques without any additional clock control circuit. A fully pipelined design can be realized by alternately applying two clock signals on neighboring stages, for instance, in an  $n$ -bit adder structure. Hence, the proposed adder's throughput can be considerably increased to one output set per 1 ns, which leads to an equivalent 1 ns delay. A larger current injection to the MG could lead to a higher computation speed, but it also leads

Table V  
COMPARISON OF FA DESIGNS.

Designs	Type	ER <sup>(1)</sup> (%)	MED <sup>(2)</sup>	MRED <sup>(3)</sup> (%)	Device count <sup>(4)</sup>	Power <sup>(5)</sup>	Delay <sup>(6)</sup>	Conf. <sup>(8)</sup>
CMOS [43]	Accurate	0	0	0	42T	71.1 $\mu$ W + 0.9nW	2200ps	No
CMOS [1]	Approximate	25	0.25	4.17	14T	32.5 $\mu$ W + 2.1nW	645ps	No
MTJ-based [43]	Accurate	0	0	0	34T+4M	2100 $\mu$ W + 0nW	10200ps	No
MTJ-based [26]	Approximate	50	0.5	29.17	21T+4M	1702.6 $\mu$ W + 329.5pW	3016.22ps	Yes
MTJ-based [26]	Accurate	0	0	0	25T+4M	1895.1 $\mu$ W + 401.6pW	3019.3ps	Yes
MTJ-based [26]	Approximate	50	0.5	31.25	25T+4M	784.5 $\mu$ W + 77.91pW	3152.7ps	Yes
SHE-based [20]	Accurate	0	0	0	23T+3SM	710 $\mu$ W + 0nW	7000ps	No
HPM DWM [19]	Accurate	0	0	0	20T+4M+2D	1364 $\mu$ W + 0nW	269ps	No
LPM DWM [19]	Accurate	0	0	0	20T+4M+2D	85 $\mu$ W + 0nW	877ps	No
Prop. FA	Accurate	0	0	0	28T+4M+2D	55.6 $\mu$ W + 0nW	3000ps <sup>(7)</sup>	Yes
Prop. FA	Approximate	25	0.25	4.17	28T+4M+2D	28.9 $\mu$ W + 0nW	2000ps*	Yes

Note: To attain a fair comparison, technology scaling is applied. (1) Error Rate. (2) Mean Error Distance. (3) Mean Relative Error Distance. (4) T: MOS Transistor, M: MTJ, SM: SHE-MTJ, D: DW. (5) Total power including write and read operations: dynamic power + static power. Power must be supplied to keep data in CMOS-based storage circuit at any time. However, it can be cut-off in the non-volatile designs. (6) Total delay including write and read operations. (7) 1000ps considering the pipeline technique. (8) Provision of approximation configurability.

to a higher power consumption. Furthermore, an embedded buffer can be presumed for spintronic devices due to their non-volatility characteristic; however, such a buffer should be inserted between every other logic gates working at different operational phases in a CMOS design. The designs in [19] also lack the appropriate input circuit such that driving transistors are needed for cascading to other cells. This point is also taken into account in the design of compressors using cascaded FAs, as evaluated next.

### B. Approximate Compressors

We have evaluated the performance of proposed approximate 4-2 compressors in terms of device count, total power and delay. Three different accurate spintronic FAs (i.e. MTJ-based [43], LPM-DWM [19] and HPM-DWM [19]) listed in Table V are used for constructing accurate 4-2 compressors as Fig. 5a. To make the counterpart designs cascadable, appropriate input transistors are added. Table VI compares their simulation results with the proposed hybrid spin-CMOS approximate compressors (as delineated via Designs I and II). It can be seen that Design I shows significant reduction in power consumption compared to other designs, with  $\sim$ 66%, 97.8% and 98.6% less power than LPM-DWM [19], HPM-DWM [19] and MTJ-based compressors [43], respectively. In addition,  $\sim$ 19% speed-up is achieved compared to LPM-DWM based compressor.

Table VI  
COMPARISON OF ACCURATE AND APPROXIMATE COMPRESSOR DESIGNS

Designs <sup>(1)</sup>	Device count	Power ( $\mu$ W)	Delay <sup>(2)</sup> (ns)
MTJ [43]	68T+8M	4200	20.4
HPM DWM [19]	46T+8M+4D	2728	2.54
LPM DWM [19]	46T+8M+4D	170.2	3.7
Design I	22T+4M+2D	57.8	3
Design II	33T+6M+3D	84.5	4

(1) Accurate compressors are designed based on the FAs in the references.  
(2) Total delay including write and read operations.

## VII. APPLICATIONS

In this section, we focus on image compression algorithms and show the results of using accuracy-configurable adder

and approximate compressor-based multipliers in such applications. Most of DSP algorithms use two basic operations: additions and multiplications. Thus, we expect that leveraging the proposed majority-based primitives could provide limited accuracy loss for improvements in other circuit metrics such as power and speed. The Discrete Cosine Transform (DCT) and Inverse DCT (IDCT) are the kernel of the international standard lossy image compression algorithm referred to as JPEG [47]. The interesting feature of DCT is that, for a typical image, most of the visually important information is concentrated in a few coefficients of DCT. One-dimensional integer DCT for an 8-point sequence  $x(i)$  is given by

$$y(k) = \sum_{i=0}^{7} f(k, i)x(i), k = 0, 1, 2, \dots, 7 \quad (8)$$

We assess the output quality of the decoded image after IDCT employing the well-known metric of peak signal-to-noise ratio (PSNR) which is based on the mean square error (MSE):

$$MSE = \frac{1}{mp} \sum_{i=0}^{m-1} \sum_{j=0}^{p-1} [I(i, j) - F(i, j)]^2 \quad (9)$$

$$PSNR = 10 \log_{10} \left( \frac{MAX_I^2}{MSE} \right) \quad (10)$$

In (9),  $m$  and  $p$  denote terms for the image dimensions;  $I(i, j)$  and  $F(i, j)$  are the exact and computed values of each pixel, respectively. In (10),  $MAX_I$  represents the maximum value of each pixel.

### A. Accuracy-Configurable Adder

To efficiently implement DCT-IDCT employing the proposed accuracy-configurable adder, each  $f(k, i)$  (i.e. cosine functions) in (8), is converted into an integer [38]. As thoroughly discussed in [1], [48], the integer output  $y(k)$  is accordingly right shifted to produce the actual DCT output. An identical expression is also presented in [48] for 1-D integer IDCT. We change the integer coefficient  $f(k, i)$  for  $k = 1 - 7$  in order that the multiplication between  $f(k, i)$  and  $x(i)$  can be equivalently implemented by two left-shifts and an addition.



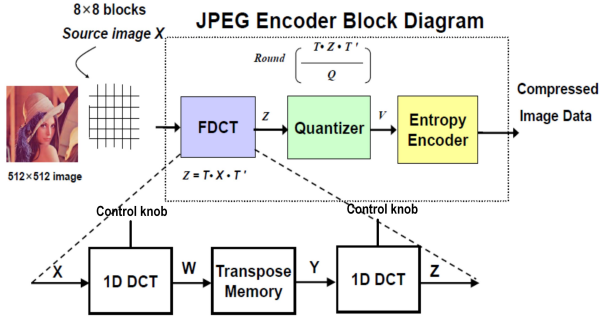


Figure 10. System block diagram of DCT/IDCT architecture.

The most significant coefficient  $f(0, i)$  is left unchanged. In this way,  $f(0, i)x(i)$  is basically the sum of 4 terms, so it can be implemented with a CSA tree by a 4-2 compressor followed by a Ripple Carry Adder (RCA). In addition, every DCT/IDCT output is the addition of eight terms that can be computed employing a CSA tree (implemented by an 8-2 compressor) followed by an RCA. Therefore, the entire DCT-IDCT system can be implemented employing RCAs and CSAs and can be approximated using the proposed adder.

We use the approximation mode of the proposed accuracy-configurable FA only in the LSBs of adders in a 20-bit DCT-IDCT architecture while exploiting the precision mode in MSBs. Accordingly, as depicted in Fig. 10, the output quality can be controlled in DCT blocks using the control knob regulating the operation mode of the proposed adders. The simulation results are obtained by using Matlab with an Intel Core i7 processor and 4GB RAM. Fig. 11 shows the processing quality of the examined image in the base case (i.e., 20-bit in precision mode), 8-, 10-, and 12-LSB cases. As shown, there is some loss of quality in the reconstructed image in Fig. 11c using approximate adders at 10 LSBs with the

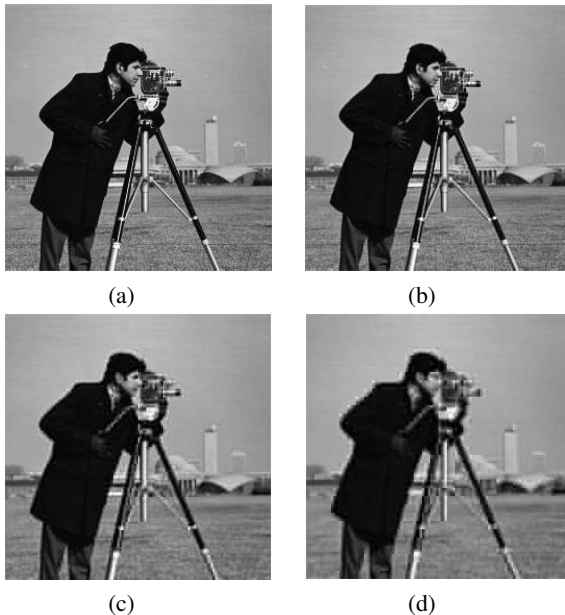


Figure 11. Compressed images and corresponding PSNR (a) Base case (33.73 dB), (b) 8 LSBs (30.82 dB), (c) 10 LSBs (26.93 dB), (d) 12 LSBs (23.75 dB).

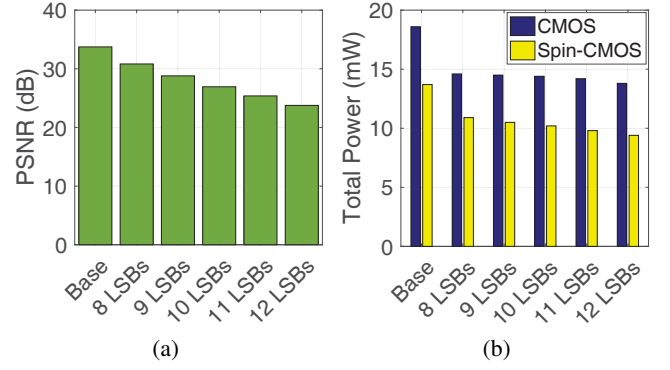


Figure 12. (a) Output quality comparison of different approximations, (b) Power consumption comparison of CMOS and spin-CMOS DCT-IDCT.

PSNR (26.93 dB), however the image is still well recognizable. Fig. 12a shows the output quality for the base case and five different degrees of approximations in PSNR. It can be seen that by increasing the approximation degree from the base case to 8 LSBs, the PSNR only drops by 2.93 dB.

The power consumption of the DCT-IDCT circuit is evaluated using Synopsys Design Compiler for both pure-CMOS and spin-CMOS circuits as depicted in Fig. 12b. For pure-CMOS and spin-CMOS circuits, a Verilog code describing the truth table in Table III is considered for implementing the approximate adder based on existing and developed cell libraries, respectively, which is then used in 8-12 LSBs of a 20-bit DCT-IDCT architecture. Simulation results show that for all cases the power dissipation of the proposed spin-CMOS architecture is smaller than the CMOS counterpart. Evidently, by changing the degree of approximation, the power consumption of the entire system is changed. For instance, 31.33% power saving is obtained for the spin-CMOS architecture with 12 approximate LSBs in comparison with the base case, although the output quality is degraded to a PSNR of 23.75 dB. In a similar scenario, 8 approximate LSBs provide power saving of 20.4%, although the output quality is slightly degraded to 30.82 dB.

### B. Approximate Compressor-based Multipliers

As mentioned earlier, in the DCT-IDCT computation, the multiplication operations can be implemented by the approximate compressor-based multipliers, while the additions remain accurate. As the DCT coefficients are in the range of  $(-1, 1)$ , they are multiplied by  $2^{15}$  to be converted into 16-bit signed binary numbers in  $2^s$ 's complement representation. Hence, the matrix multiplication in DCT and IDCT are implemented by  $16 \times 16$  approximate signed multipliers. To obtain the best trade-off, different configurations of  $16 \times 16$  approximate signed multipliers are employed for the matrix multiplication in the DCT and IDCT algorithms. A configuration means using the proposed approximate 4-2 compressors for the accumulation of a different number of columns of least significant partial product bits. The signed multiplier is implemented by using the Baugh-Wooley algorithm, thus, a similar partial product array is obtained as the unsigned multiplier. As in [13], the partial products of the signed multiplier are accumulated

Table VII  
COMPARISON OF THE ACCURATE AND APPROXIMATE COMPRESSOR-BASED MULTIPLIERS FOR DCT-IDCT

Design	Accurate	Approximate (32 bits)		Approximate (16 bits)		Approximate (13 bits)		Approximate (12 bits)	
		Design I	Design II	Design I	Design II	Design I	Design II	Design I	Design II
PSNR (dB)	Inf	4.0948	4.0948	13.0542	14.1232	37.0205	37.8094	50.2156	50.9583
Delay reduction ( <i>n.s</i> )	-	108.89	102.19	85.64	80.44	75.08	73.25	69.56	66.71
Energy reduction ( <i>m.J</i> )	-	140.24	118.05	91.12	89.99	80.16	77.29	74.44	71.73

by a Dadda tree. The accurate addition is implemented using the proposed accuracy-configurable adder in precision mode. We run the experiment using the approximate compressors at all, half (16), 13 and 12 LSBs of the multipliers. Fig. 13a shows the accurate results for the DCT-IDCT implementation. The results of using approximate compressors on half and 12 LSBs are shown in Fig. 13b and Fig. 13c, respectively.

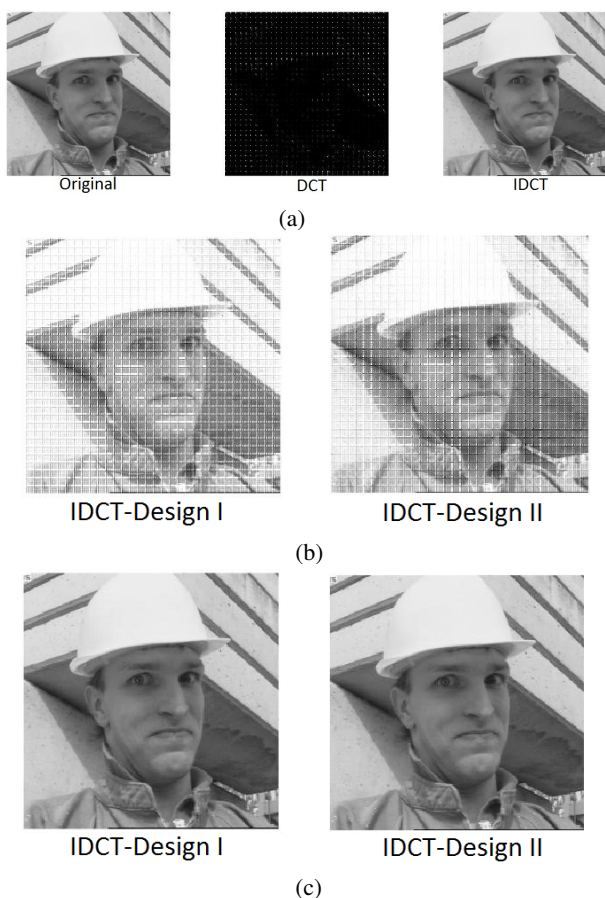


Figure 13. DCT-IDCT results of using (a) accurate compressor, (b) approximate compressors in half LSBs (16 bits), (c) approximate compressors for 12 LSBs.

The reconstructed images reveal that using the approximate compressors for all partial product bits or half LSBs cause image distortion, while the reconstructed images using approximate compressors on 12 LSBs show a similar quality with the accurate result. The defects in the image generated by the multiplier using approximation on the half (Fig. 13b) and 13 LSBs are visible after zooming in. The PSNR values provided in Table VII indicate the same conclusion. The delay and energy reduction of using approximate compressor-based multipliers

compared to accurate MTJ-based multiplier [43] are also listed in Table VII. The total number of approximate compressors used in different configurations is obtained to evaluate the respective energy reduction. As for delay reduction, the total number of approximate compressors in the critical path is obtained. The results indicate that the DCT/IDCT systems using the approximate compressor-based multipliers achieve  $\sim 50\%$  reduction in energy consumption and 3x speed-up compared to the exact circuit with a comparable output quality. Obviously, by sacrificing the quality, system attains even higher energy-efficiency and speed-up. It is noteworthy that in all cases, the multiplier which is based on Design I has provided better result in terms of energy and delay with lower PSNR as compared to that of Design II.

## VIII. CONCLUSION

In this paper, a compact and energy-efficient accuracy-configurable adder design and two approximate compressors based on a composite spintronic device structure have been developed and assessed. Based on the majority logic, the proposed designs can be effectively utilized to trade off computation energy for more fluid levels output quality in DSP systems. A device-to-application simulation framework has been constructed and shown to be effective to evaluate the proposed hybrid spin-CMOS circuits. Furthermore, the proposed accuracy-configurable adder and approximate compressors are efficiently-utilized in a DCT block to fully-realize a widely-used digital image processing algorithm. The results indicate that the DCT/IDCT using an approximate multiplier achieves  $\sim 50\%$  energy consumption while attaining roughly 3x speed-up compared to the exact MTJ-based design with a comparable accuracy.

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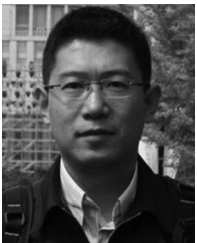


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